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Program Office	ТТМ	Proposal No.	Topic No.	
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TO BE COMPLETED BY PROPOSER

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Title of Project

MINIMIZE MARINE PIPELINE OIL SPILL

Technical Abstract (Limit to two hundred words)

The scope of this Phase I research was to determine how environmental risks can be decreased and how the safety of personnel and property can be increased with offshore pipelines. This work shows how the objective can be achieved by a better material specification. When a marine pipeline is accidentally damaged by boat or ship anchor drag or by impact by fishermen trawl boards, the pipeline gets dented which can cause the line to collapse and then buckle with the buckle propagating down the line. In the process the line usually ruptures causing an oil spill or a gas leak. With a proper specification of the ultimate elongation of the steel, the pipe will stretch but not rupture during the collapse and buckling process.

Anticipated Results/Potential Commercial Applications of the Research

The Phase I results can be used now as rough guidelines. development work is needed to refine the procedures and for experimental confirmation of the theory. The anticipated results of the development work are that the oil, pipeline, and construction companies can use the procedures for improved steel pipe specification and DOI personnel can use the procedures for advice and counseling to industry. Implementation of the development work will result in safer pipelines and less environmental risk at no or negligible additional cost.

The views and conclusions contained in this document are those DISCLAIMER: of the author and should not be interpreted as necessarily representing the official policies or recommendations of the Department of the Interior.

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INTRODUCTION

This project was a Phase I research effort performed through the SBIR (Small Business Innovative Research) Act passed by Congress and administered through the MMS (Minerals Management Service) in the U.S. Department of the Interior. The idea of SBIR is to get small business a little more involved in federally funded programs to expand our general technology base and to provide more jobs by commercial implementation. The program then consists of initial Phase I research efforts, a more comprehensive Phase 2 development effort by a few of the most viable participants in Phase 1, and then hopefully a Phase 3 commercial implementation without any federal funding.

The scope of this reported research was concerned with both environmental concern and personnel safety with offshore pipelines. These marine pipelines run between fixed offshore oil and gas production platforms and from the platforms to shore. The specific scope of this work was to ascertain considerations to minimize leaks in offshore pipelines.

We occasionally experience pipeline leaks due to a large variety of reasons as discussed in the next section. Fortunately, the number of leaks and amount of oil spilled is extremely small relative to amount of oil handled by marine pipelines. But we should strive to do better and make the efforts cost effective in the process. For example the cost of this research work is insignificant relative to the cost for cleaning up any one large oil spill.

Some of the major sources of marine pipeline leaks are damage by boats dragging anchor over a line or by fishing trawl boards banging the line. The resulting ding could initially rupture the line, or damage it so that it later fails when fully pressurized, or the protective coating could be damaged so that the line fails later by corrosion.

When an oil line leaks, it temporarily messes up the environment and is

sometimes bad news for birds and fish - but virtually no danger to personnel will ensue. Conversely, with a gas line leak, there is no detectable damage to the environment, but if the line were near a platform, it is possible that this could lead to an explosion with significant loss of life and property.

Our approach here then is to figure out how that we can be reasonably sure that a damaged line will stretch but not rupture when it collapses. The way to do this is to first understand the geometry and mechanism of the failure mode of the pipe. Then we can predict the required elongation or stretch of the steel used in the pipeline.

We have done that in this report with the calculations shown for the preliminary theoretical procedures. The work shows that we should choose the type of steel for a particular pipeline based on internal operating pressure of the fluid being pumped, the external water pressure based on depth from the ocean level down to the mudline, and the pipe diameter and wall thickness.

It required some rather fancy engineering as outlined in this report to accomplish the objective. But the work was boiled down to a simple equation that can be used for steel mill specifications on a tentative basis. Experimental work will be required for verification and to improve the approximations.

Seems like the work discussed in this report should be of interest to various design engineers in several segments of industry such as oil and gas companies, marine pipeline construction companies, and the pipeline operating companies. More importantly this work will give MMS personnel a better understanding of pipeline failure mechanisms. With this additional knowledge MMS personnel should now be in a position to offer advice and counsel to industry during the review stages for new marine pipeline construction.

For the benefit of those readers that are not involved in marine pipeline work, a schematic of a barge depicting the system used to construct an offshore pipeline is shown in Chart 2-1. Drawing on our previous marine pipelay design work, the specifics for an example to show the influence of water depth is shown in Chart 2-1 with the results from the structural analyses shown in Chart 2-2.

OIL SPILL STATISTICS

From MMS data (Chart 3-1), there were 30 major spill incidents (greater than 238 bbl/incident) in the years 1964 through 1981 in the OCS Gulf of Mexico from all sources. In this time frame the number of offshore structures (platforms and satellites) increased from 1,100 to 2,744 (average 1,922) while annual oil production increased from 115 to 228 million bbl (359 peak in 1971) or accumulative 4,632 million bbl. These numbers equate to average 175 bbl spilled per structure and 13,791 barrels produced per bbl spilled.

In their very comprehensive treatise published Dec 77 on offshore pipeline safety practices, Funge et al (F5) collected extensive data on causes and volumes of oil spills. Their summaries are given in attached Charts 3-2 through 3-11 for the convenience of the reader with only the following brief comments. As an aside, extensive data is available from DOI and DOT for an update but the given information was considered sufficient for present purposes.

In all of the major accidents on the OCS involving 1,000 bbl or more spilled in the years 53-72, only four of the 43 total incidents were caused by pipeline ruptures but these four incidents accounted for over half of the oil spill volume (Chart 3-2). In the years 67-76, there were 22 pipeline spills of 50 bbl or more in OCS waters, one due to corrosion and six due to external impact of anchor drag, dredging or trawl boards (Chart 3-3). In the years 71-75 on the Gulf of Mexico OCS, oil spills of 50 bbl or less due to pipeline leaks and ruptures accounted for about 10% of the total number of spills and about 12% of the spill volume (Chart 3-6). The statistics on liquid pipeline spills onshore and offshore U.S. for the years 68-76 are given in Charts 3-9,10 with similar tabulations for gas pipelines in Chart 3-11.

CODES AND REGULATIONS

As shown by the most current Code of Federal Regulations (C1), the maximum design factor for offshore oil or gas pipelines is 0.72 based on SMYS, or a 1.4 safety factor. This also corresponds with the minimum safety factors specified in the various codes used in West European countries (P8), as shown by Chart 4-1.

The minimum test pressure is then taken as the sum of the external pressure plus 1.25 times the internal design pressure, IDP. The maximum internal pressure minus the minimum external pressure gives the internal design pressure. This API criteria (A14) is based on the ANSI piping standards (A8,9).

After a marine pipeline is installed and in operation it can incur damage due to several causes. Some areas in the Gulf of Mexico have big problems of soil fluidization and then transport with agitation by storm waves. Subsequent soil depressions leads to pipe bridging and the pipeline can then fail in fatigue because of the induced oscillations (H6).

In areas of heavy fishing activity the pipeline can become dented as trawl doors hit the line (G3). For this reason most offshore areas with fishing activities now have some type of pipeline burial requirement (M8), as shown in Chart 4-2.

At the present time neither DOT nor MMS have any regulations regarding allowable stress and strain during pipelay or repair operations. The applicable codes and regulations are concerned with adequate structural integrity of marine pipelines under stated normal operating conditions. As a consequence there are no codes or regulations that indicate desirable material property magnitudes to insure dry versus wet buckles or collapse.

DESIGN FOR OFFSHORE PIPELINE CONSTRUCTION

Some of the most important factors to be considered for laying offshore pipelines have been studied using a finite element program and these results were published in the literature (B5-B12). In another published study (B4) the available literature was reviewed and equations summarized for elastic hydrostatic collapse with and without out-of-round, plastic hydrostatic collapse pressure, and elastic buckling with combined loads. Design Chart 5-1 gives the maximum allowable bending moment as a function of water depth, and pipe diameter, wall thickness, and yield strength.

In a related paper (B22) the material properties as specified by the API Codes were summarized (Charts 5-2,3) for convenient reference during design. That paper also gave a number of other convenient design charts such as specific gravity for various sizes of pipe and concrete thickness, allowable water depths as a function of pressure, flexure, pipe dimensions, coating thickness, etc.

Haagsma (H8) reported some theoretical procedures to account for pipe out-of-roundness and to show the interaction between external pressure and either pure tension or bending. The essence of that work is given in Chart 5-4. This shows that the influence of out-of-round is greater for the lower D/t values, and that the allowable pressure is reduced more with pure line tension than with bending.

PIPE PROPERTIES

When trawl doors strike a marine pipeline for example, it would be more desirable that the pipe dent rather than crack. From this viewpoint a material with a higher toughness would be desirable. Charts 6-1,2 show the variation of charpy values reported by two manufacturers, Italsider (C6) and Kawasaki (U1), of API 5LXX70 pipe. Note that the charpy values increase with decreased sulfur content. While API specs give the minimum requirement for percent elongation in two inches, values of 36 to 44% have been reported in the literature (V1) for grades X65 and 70.

The design properties of API pipe are given in Charts 6-3,4. Pipe volumes are given in Chart 6-5.

PIPE COATINGS AND CATHODIC PROTECTION

Marine pipelines are normally protected with an organic coating in combination with cathodic protection. A concrete coating is then applied over the corrosion protection coating for weighting and stability purposes.

The six most often used corrosion protection coating materials are coal tar enamel, asphalt enamel, asphalt mastic, thin film powdered epoxy, bonded polyethylene, and various tape wraps. A survey of pipeline coatings was performed by O'Donnell (01) and his results are shown in Chart 7-1. This work shows that coal tar enamels are most often used. Adhesion was considered slightly more important than resistance to cathodic protection, and penetration resistance the third most important coating property. The tabulation of physical properties of pipeline coatings prepared by Askheim and Eliassen (A19) is given in Chart 7-2.

The current requirements and the capacity of anodes per NACE and discussed by Rizzo (R6) are given in Chart 7-3. Using DNV rules (Norway), Mollan and Eliassen (M9) reported a design procedure for spacing anodes on a marine pipeline and their technical data is given in Chart 7-4.

VALVES TO REDUCE OIL SPILL

When a marine pipeline fails it is possible for a buckle to propagate. Whether a wet buckle (pipe wall ruptures) or a dry buckle results depends upon the material properties of the pipe. As a contingency to minimize wet buckle oil spills, remote actuated valves have been installed in marine pipelines during pipelay operations. But sometimes a pipeline rolls as it is going over the stinger and the valve operator could be orientated upside down in the mud after being laid. In that case the valve could not be remotely closed.

If it is known sufficiently ahead of time that a very severe storm is going to pass through a pipeline lay barge location, the normal procedure is to abandon the pipeline. After the storm has passed the pipeline is retrieved and pipelay operations then continued. But this is an expensive operation. If the weather prediction is for a relatively mild storm, it may be decided to cease lay operations but to hang on to the pipe in the tensioners. This or relatively large vessel heave values can cause some small amount of plastic strain in the line due to dynamic flexure. Some weather design criteria for various offshore areas of the world are given in Chart 8-1.

As shown schematically in Chart 8-3 the reason that a pipeline will roll during lay operations is because the total energy of elastic and plastic strain in the pipeline is reduced with torsional rotation. The problem has been solved for a 60 ksi yield steel using the constructed stress strain diagram and the computed strain stress equations shown in Chart 8-2. Knowing the anticipated pipeline roll, the valve can then be placed in the joint at a prescribed angle so that it will be vertical when it reaches the mudline. An operations chart for this purpose is shown in Chart 8-3 for a 60 ksi steel.

NONLINEAR STRESS-STRAIN RELATIONS

An accurate prediction of pipeline collapse must take into account the nonlinear stress-strain relation of the steel in the plastic response after the yield strength has been exceeded. This behavior is peculiar to each type of steel and must be determined from uniaxial lab tests. A procedure and the results are given here for use in preliminary work when the actual mechanical properties of the steel being considered has not been tested. To do this we have utilized the reported tests by Brittain (B13) on a variety of different steels. Importantly, Brittain gave true rather than engineering values, and the essence of his work is summarized in Chart 9-1.

Most labs usually report their material property tests in terms of engineering values. Engineering stress is the force at any time during the test divided by the original cross sectional area of the test speciman. True stress is the applied force divided by the true necked down area at that time, so true stress is greater than engineering stress values in the plastic response. The true strain is the differential stretch divided by the instantaneous stretched length rather than the original length of speciman used to calculate engineering strain. Hence the true strain is less than the engineering strain in the plastic response. The equations for converting between true and engineering values as well as the definition of the strain hardening coefficient are given in Chart 9-2, and the significance of the differences is shown in Chart 9-4.

What we have done is mess around with the data in Chart 9-1 which is shown to be linear plots on log-log paper. Taking the standard equation functional for this type of relationship and the API definition of 0.5 percent strain at yield leads to the data points in Chart 9-3 for the constants K and n.

An example comparison is shown in Chart 9-4. The derived strain hardening coefficient using Ref. VI data is 0.15 versus 0.17 using our linearized coefficients shown in Chart 9-3.

ELASTOPLASTIC BEAM BEHAVIOR

To get to the problem of determining maximum strain in a pipe at collapse, we have to know a little bit about plastic structural analyses. In our first approximations we will also use beam theory. For the benefit of those engineers that do not perform plastic structural analyses every day, the basic theory for our procedures is given here.

Chart 10-1 gives the equations for various load types and beam end conditions for use in regular elastic analyses. When a sufficiently large moment is applied to exceed the yield strength, the beam moment versus curvature becomes nonlinear as the so-called plastic hinge point is formed as shown in Chart 10-2. The problem with all of the good textbook theory on plastic analyses is that the strain theoretically becomes infinite when the fully plastic moment has developed. That is no problem in ordinary structural analyses where the induced stresses are compared with allowable code stresses. But here we are interested in the strain values for use in material specifications and we cannot massage infinity.

Chart 10-3 gives the derivation of the fully plastic moment for a beam having a rectangular cross section. The results show that the fully plastic moment is 1.5 times the value of the maximum elastic moment. While the elastic moment varies nonlinearly along the beam length, Chart 10-4 shows that the moment varies linearly for all practical purposes from the point of maximum elastic load to the point of maximum plastic moment at the ends of a fixed end beam with uniformly distributed load. This is a key input to our collapse pressure derivation to get the maximum induced strain.

Chart 10-5 gives the derivation of the extent of plasticity at a hinge as a function of the beam curvature. These relations are required to study the intermediate stages of pipe collapse.

ELASTIC AND PLASTIC STRAIN ENERGY

The general three-dimensional equations of elasticity in rectangular coordinates are given in Chart 11-1. This includes the conversions between stress and strain using Young's modulus and Poisson's ratio for the three dimensional as well as the plane stress and plane strain cases.

The amount of internal energy stored in the structure (beam, shell, etc.) is called the strain energy. Chart 11-2 gives the total strain energy in terms of stress and in terms of strain for the general three dimensional stress state as well as for the case of plane stress.

The thing gets a little more complicated when the yield stress is exceeded. The strain energy is then the sum of the stored elastic energy plus the dissipated plastic energy. Chart 11-3 gives the equation of the plastic strain energy for a beam in terms of strain hardening coefficient of the material.

The resulting integral is not common. One way to solve the functional is to use a binomial expansion, multiply the terms, combine the units, then integrate each resulting integral in the sum of terms. The series of integrals is continued until the desired degree of accuracy is obtained, to wit, addition of remaining integrals beyond the truncation point would not significantly effect the results. This is not amenable to hand calculation but the problem could easily be handled with a computer when doing final design work.

VON MISES AND AISC FAILURE CRITERIA

The six commonly accepted bases of material failure are (1) maximum principal stress, (2) maximum shear stress, (3) maximum principal strain, (4) maximum shear strain, (5) total energy, (6) distortional energy. These failure modes are listed in order of ease of usage and hence engineering popularity. However, for structures under three dimensional stress, the precision and applicability would be given in reverse order.

The equations for the distortional energy basis, more commonly called the Von Mises criteria, for a triaxial stress state are given in Chart 12-1 in terms of stress and in terms of strain for elastic and plastic analyses. This shows that the equivalent uniaxial yield strain allowable is 33% greater in plasticity relative to an elastic state.

The pipeline considered in triaxial state versus biaxial stress is explained in Chart 12-2. This shows the allowable stress by Von Mises would be about 26% greater than permitted by the simplified ordinary analyses.

A laid section of pipeline is not free to expand longitudinally and the effect of this restraint is studied in Chart 12-3. Using the AISC Code procedures, the restraint would have negligible effect in contradistinction to the Von Mises approach.

COLLAPSE MODES AND PROPAGATION PRESSURE

When a pipeline has a dent in it or if the pipe is sufficiently out of round, then at a certain pressure the pipe will plastically deform radially inward and buckle longitudinally. If the pressure load is greater than the amount of stored elastic energy plus dissipated plastic energy, then the buckle will propagate along the length of the pipeline.

The amount of pressure to make the buckle propagate depends upon the failure mode. With a constant wall thickness along the pipe the collapsed state will look sort of like a figure 8. The derivation of an equation to predict the propagation pressure for an eight collapse is given in Chart 13-1.

If a pipeline is banded such as with a buckle arrestor ring, the pipe is then restrained from failing in the eight collapse. As the buckle propagates it then jumps through an unwelded arrestor ring in the collapse mode shown in Chart 13-2 and here called a nest collapse. As shown by the derivation in Chart 13-2, the propagation pressure for a nest collapse is approximately two times the propagation pressure for an eight collapse.

The various computed pressures for a couple of laid pipelines are shown in Chart 13-3 for examples. The computed pressures in psi for the first example were 223 due to external water pressure at the 500 foot depth, 920 for failure by external pressure, and 109 for a buckle propagation in an eight collapse mode. This means that if the pipe is sufficiently dented to cause a buckle in 500 feet of water, then without the use of buckle arrestors the buckle would progress along the length of the pipeline until a depth was reached where the propagation pressure is less than the water pressure, or to a water depth of $500 \times 109/223 = 244$ feet.

MAXIMUM STRAIN IN COLLAPSE MODE

It is now time to combine all of the previous information given to come up with something we can work with. The procedure is to equate the external work function with the internal strain energy. The elastic internal strain energy stored is very small compared to the plastic internal strain stored dissipated so we will neglect the elastic energy here. Chart 14-1 gives the relation for the external work after a complete figure eight collapse for one-fourth of the pipe.

Chart 14-2 gives the assumed strain variation at each quarter point or plastic hinge formed in the pipe after complete collapse. This strain functional is given in terms of the variation radially from the neutral axis and circumferentially from the hinge point. The functional is then integrated across each side of the equivalent beam at each end of a quarter section of the pipe with the results given in Chart 14-3.

The external work from Chart 14-1 is equated to the plastic strain energy from Chart 14-3 to obtain the relation of the expected maximum strain at the hinge as shown in Chart 14-4. Since the yield stress appears in both the work and the energy, this term drops out so the maximum strain is not a function of the yield strength. After the biaxial effects are taken into account using Von Mises strain criteria, the final result is that the maximum estimated strain at collapse is 12.75 divided by the pipe diameter to thickness ratio. Simple enough.

Using data from the published literature on a couple of laid pipelines, the first shows a 30.7% strain requirement and the second shows a 62.5% strain requirement. These are the ultimate strain values the material should have as determined by a uniaxial tensile test so that the installed pipeline completely failed in a figure eight collapse will have stretched without rupture.

BUCKLE PROPAGATION AND ARRESTORS

The ratio of critical pressure for collapse due to external pressure on a round pipe compared to the buckle propagation pressure is discussed in equation form in Charts 15-1,2. This shows why a buckle in a pipeline will propagate until much more shallow water depth is reached or until the buckle runs into a thicker section such as at a buckle arrestor or a line valve.

In practice the critical/propagation ratios are lower than the theoretical predictions because the formulas are for perfectly round pipe. Some out-of-roundness is allowed for the steel mill per ASTM and AISC codes since it is not practical or even possible to find perfectly round pipe.

The pipe buckles and the buckle propagates because of gross out-of-round or a ding due to unplanned damage to the pipe as previously discussed. The radial velocity of the buckle propagation is a function of the pressure head, i.e. the difference between the external water pressure and the propagation pressure as illustrated in Chart 15-3. The longitudinal velocity of the buckle propagation is a function of the yield stress, pipe diameter, and pipe wall thickness. The buckle shape will find a configuration for minimum plastic strain energy per unit length of additional deformation.

The size and type of buckle arrestor ring to use depends upon technical and economic considerations. Normally, a welded arrestor is better than a grouted arrestor since the buckle can jump through the grouted arrestor as shown in Chart 15-4. However, grouted arrestors would be appropriate if the jump through pressure exceeded the external water pressure, i.e. for the case of very shallow water depths.

CONCLUSIONS

- 1. This project was concerned with both pipeline safety and environmental considerations by decreasing the possibilities of offshore pipeline leaks as a result of damage to the laid line due to anchor drag, dings by fishermen trawl boards, etc.
- 2. The approach was to determine a suitable minimum mechanical property specification, to wit, ultimate elongation, so that a damaged pipeline could collapse and in the process, stretch but not rupture.
- 3. If the pipeline does not rupture at collapse, this will preclude oil spills and consequential damage to the birds, the fish, and the beaches. For the case of gas pipelines where failure has inconsequential environmental effects, a collapsed gas line without rupture near an offshore platform or terminal facilities greatly improves the safety for people and property.
- 4. Using some simplified assumptions in this Phase I work, the results were that the minimum ultimate elongation as determined from a uniaxial tensile test on the material to be used in a planned pipeline should be equal or greater than about 12.7 divided by the diameter to thickness ratio of the pipe.
- 5. The greater the strain hardening coefficient of a candidate steel, the more the determined minimum ultimate elongation can be decreased as long as the Charpy or Izod values are not adversely affected.
- 6. The results given in this report can be used as guidelines now. Before implementing the results into a final specification or technical requirement, the approach should be refined by including the effect of the strain hardening coefficient, etc.

RECOMMENDATIONS

- 1. Laboratory tests should be performed to confirm the theory presented in this report.
- 2. To reduce the cost of the lab tests, this should be done primarily with line loads applied to sections of pipe with only a few of the more expensive tests performed using external pressure loading.
- 3. Similar theoretical treatment of line load application will be required to confirm the theoretical line load/pressure load analog, the experimental line load/pressure load analog, and finally the theoretical pressure load/experimental line load analog.
- 4. The required ultimate elongation properties should be discussed with personnel in the metallurgical labs of several steel pipe companies to ascertain whether or not they have a steel chemistry formulation that has the desirable characteristics and which can be produced at negligible additional cost.
- 5. Complete mechanical property evaluations and test results should be obtained from the steel mills, including minimum yield strength, maximum tensile strength, ultimate elongation, strain hardening coefficient, and charpy results for candidate steel comparisons.
- 6. Equations should be developed for determining the conditions of suitability of the less expensive type of grouted buckle arrestors.
- 7. Equations should be developed for determining the economics and cost effectiveness of both grouted and welded buckle arrestors.
- 8. The above should be performed with the <u>objective</u> of improving safety to personnel and property as well as achieving decreased risk of environmental damage at minimum or no additional costs by working smarter with a better technology base.

NOMENCLATURE

Symbol	Variable	Typical Units
A C D E	area one-half of pipe wall thickness pipe diameter Young's modulus of elasticity gravitational constant	sq. in. in. in. psi ft./sec. ²
H h I L M	water depth arrestor wall thickness area moment of inertia length of pipe secant moment	ft. in. in. ⁴ in. inlb.
n P R t V	strain hardening coefficient pressure radius of curvature pipe wall thickness volume	numeric psi in. in. cu. in.
v W x y Z	velocity external work radial coordinate circumferential coordinate area section modulus	in./sec. inlb. in. in. in.3
Bubbe	propagating buckle angle Poisson's ratio stress density of material strain	deg. numeric psi p c f in./in.
	internal strain energy	inlb.

Subscripts

a	arrestor	i	initiation	R	radial
С	critical	L	longitudinal	u	ultimate
d	dissipated	N	nest propagation	W	water
e	external	P	propagation	y	yield

LIST OF ABBREVIATIONS

AIAA American Institute for Aeronautics and Aerospace Journal

AIMMPE American Institute of Mining, Metallurgical, and Petroleum Engineers

AISC American Institute of Steel Construction

ANSI American National Standards Institute

API American Petroleum Institute

ASCE American Society of Civil Engineers

ASME American Society of Mechanical Engineers

CAS Computers and Structures (Pergamon Press, UK)

DNV Det Norske Veritas

DOE U.S. Department of Energy

DOI U.S. Department of the Interior

DOT U.S. Department of Transportation

EM Experimental Mechanics

EMD Engineering Mechanics Division (ASCE)

GPO U.S. Government Printing Office

IJPVP International Journal for Pressure Vessels and Piping

IJSS International Journal of Solid Structures (Pergamon Press Ltd., UK)

JAM Journal of Applied Mechanics (Trans. ASME)

JAS Journal of the Aerospace Sciences

JEI Journal of Engineering for Industry (Trans. ASME)

JEMT Journal of Engineering Materials and Technology (Trans. ASME)

JERT Journal of Energy Resources Technology (Trans. ASME)

JMES Journal of Mechanical Engineering Science

JPT Journal of Petroleum Technology (SPE)

JPVT Journal of Pressure Vessel Technology (Trans. ASME)

JSD Journal of the Structural Division (Trans. ASCE)

MCET Mechanical and Chemical Engineering Transactions, Inst. of Engineers,

Australia

MMS Minerals Management Service (DOI)

MT Marine Technology

N Number

NACE National Association of Corrosion Engineers

NSC Nippon Steel Corp., Kanagawa, Japan

NTIS National Technical Information Services

NYAS Transactions of New York Academy of Sciences

OCS Outer Continental Shelf

OE Ocean Engineering (Pergamon Press Ltd., UK)

OEM Ocean Engineering Magazine

OGJ Oil and Gas Journal

OI Ocean Industry

OM Offshore Magazine

OTC Offshore Technology Conference (held annually first week in May in

Houston, Texas)

PD Petroleum Division (ASME)

PE Petroleum Engineer

PGJ Pipeline and Gas Journal

PLI Pipe Line Industry

PRADS International Symposium on Practical Design in Shipbuilding

PT Petroleum Times

PVPD Pressure Vessel and Piping Division (ASME)

p Page

QAM Quarterly of Applied Mathematics

SMI Sumitomo Metal Industries Ltd., Osaka, Japan

SMYS Specified Minimum Yield Strength

SPE Society of Petroleum Engineers

V Volume

WRC Welding Research Council

ZAMM Zeitschrift für Angewandte Mathematek und Mechanik

KEY WORD INDEX OF REFERENCES

Blowouts: H5

Buckle Propagation: B14, C2, I1, J3, K3-8, P1

Buckling, General: T4

Casing Collapse: A15, C5, H2, K2, N1, P2, P3, S1

Catalogs: P8

Catenary: D4, I2

Coating Properties: A19, O1

Coatings, Weight: B22

Codes: A6-14, A18, B22

Combined Load Buckling: B4, C3, C4, E1, F1, F2, F4, H8, J2, K1, K2, N2, P3, P4, R1,

R2, R4, S6, T1, T2, W2, W3

Compression Buckling: A1, D1, H3, P5, T3, Y2

Construction: B20, M8

Corrosion Protection: M9, R6

Directories: P8

Elasticity: B13, N5, W4

Fatigue: B21

Flexure Buckling: A2, B22, F3, G1, H8, J1, R2, R3, S2, S3, S5, W1, W5, Y3

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Pipelay Theory: B2-12, B4, B20, D5, H4

Pipeline Accidents: M4, M6

Pipeline Failures: G3, H6

Piping Design: P7

Plastic Design: A2, A16, A17, B14, B20, H7, N5, S8, W3

Plasticity: B3, B13, B14, B20

Platforms: B19

Pressure Buckling: A4, B22, H1, H8, K9, K10, N3, N4, S4, S7, P6, Y1

Pressure Burst: R5

Production, Offshore: B16, B18

Riser Design: B3

Safety: F5

Special Studies: B20, D2

Stiffened Cylinder Buckling: E1, M1, M2, P5, R1, S7

Stinger: D5

Temperature Buckling: A1, C4

Weather: B15, B21

Wells, Offshore: B17, B18, B19

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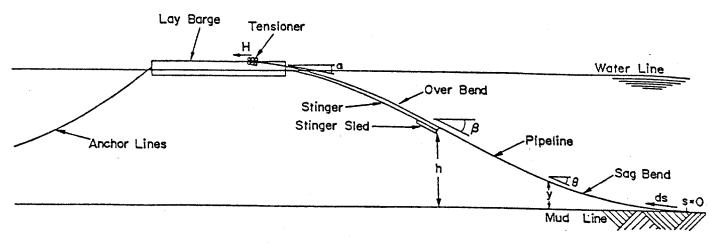
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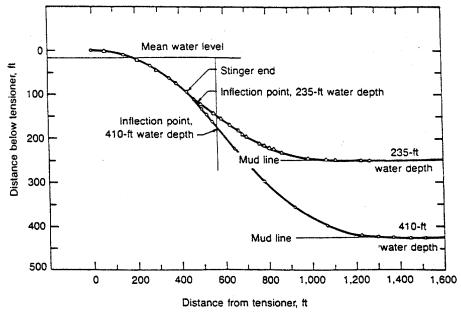
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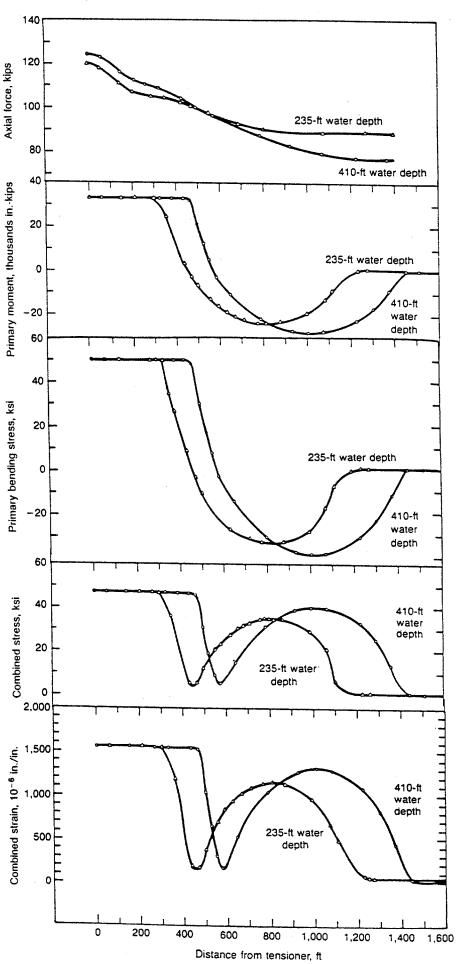


Variables for water depth

234 and 410 ft	Water depth from mean water level to mud line
120 and 124 kips	Barge tension
15 ft	Distance from tensioner to mean waterline
1,000 ft	Curved stinger radius
36 in.	Pipe outside diameter
0.75 in.	Pipe wall thickness
3.5 in.	Pipe coating thickness
734 lb/ft	Weight of coated pipeline in air
89.3 lb/ft	Weight of coated pipeline in water
7.66	Specific gravity of steel
2.33	Specific gravity of coating
3.45	Specific gravity of coated pipeline in air
1.17	Specific gravity of coated pipeline in water
$30 \times 10^{3} \text{ ksi}$	Young's modulus of the pipe
0.3	Poisson's ratio of the pipe
50 ksi	Allowable stress in the pipe



Pipeline coordinates



OIL SPILL INCIDENTS OF 238 OR MORE BARRELS OCS-GULF OF MEXICO

Calendar Year	Incidents	Oil Spilled	Number of Structures	Annual OCS Oil Production
1964	5	14,928 barrels	1,100	115 million barrels
1965	2	2,188 barrels	1,200	136 million barrels
1966	0	None	1,325	175 million barrels
1967	1	160,639 barrels	1,450	206 million barrels
1968	1	6,000 barrels	1,575	250 million barrels
1969	4*	10,624 barrels*	1,675	285 million barrels
1970	3	83,895 barrels	1,800	312 million barrels
1971	1	450 barrels	1,891	359 million barrels
1972	0	None	1,935	356 million barrels
1973	4	22,175 barrels	2,001	342 million barrels
1974	2	22,046 barrels	2,054	316 million barrels
1975	0	None	2,079	288 million barrels
1976	2	4,300 barrels	2,096	281 million barrels
1977	2	550 barrels	2,248	250 million barrels
1978	0	None	2,327	255 million barrels
1979	1	1,500 barrels	2,420	246 million barrels
1980	1	1,456 barrels	2,554	232 million barrels
1981	1	5,100 barrels	2,744	228 million barrels**
Total	30	335,851 barrels	2,744	4,632 million barrels

^{*}Revised 3/82 - Previous value, for 1969 30,024 barrels, included two spills which were not in OCS Gulf of Mexico.

SOURCE : MMS , NOLA

^{**}Preliminary value

MAJOR ACCIDENTS ON THE U.S. OUTER CONTINENTAL SHELF (1953 - 1972)

RESULT			CAUSE			
<u> </u>	Drilling	Production	Pipeline	Collision	Weather	Total
Accident Affecting: Oil Oil and Gas Gas Other Total	0 2 17 0	3 7 2 3 15	4 0 0 0 0 4	1 0 0 1 2	3 0 0 0 3	11 9 19 4 43
(a) Oil Spills of Above: Number Volume- (Thou. Barrels)	2	10 84-135.4	(b) 4 175	2.6	3 9.2-9.7	20 290-1,100
Tragedies: Deaths Injuries Fires Major Damage	23 7-8 7	33 91-100 12	0 0	0 0 1	0 0	56 98-108 20
to Platform Rig Duration	2 hrs	9 10 min 4.5 mos.	0 1-13 days	2 s l day	0 1-3 days	15 10 min.— 5.5 mos.

- (a) spills of about 1,000 barrels or more in OCS waters
- (b) Four pipeline spills are:

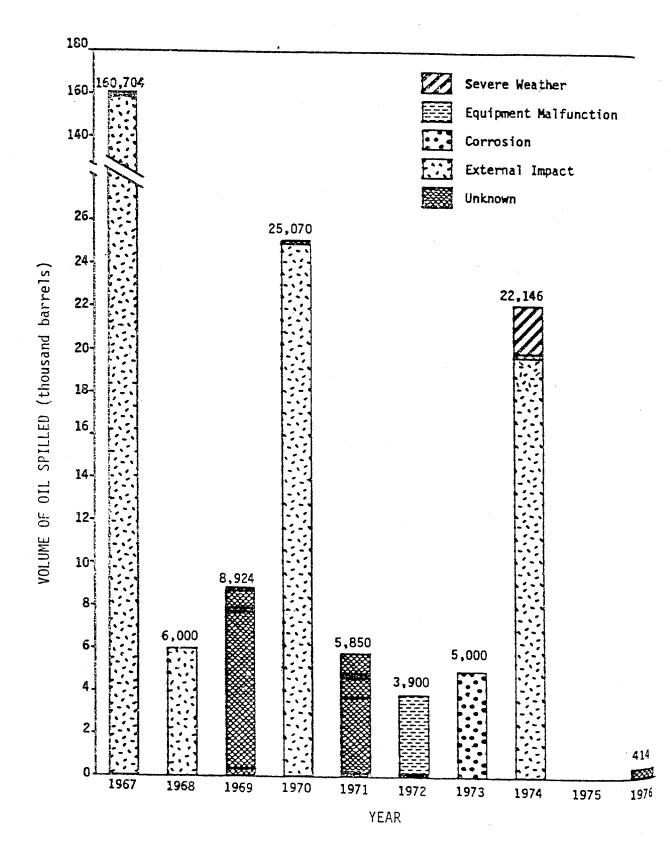
	West Delta Blk. 73	160,639 bbls.
March 12, 1968	So. Timbalier Blk. 131	6,000 bbls.
	Main Pass Blk. 299	7,532 bbls.
December 16, 1969	Santa Barbara Channel	900 bbls.

ANALYSIS OF DATA BASE OF OIL SPILLS FROM U.S. OFFSHORE PIPELINES (a)

-	-		. •								10.	10-YEAR CUMULATIVE DATA	TIVE DAT	
	•			Ď	IIME CDII	VOLUME SPILLED (bb)s)					VOLUME	VOLUME OF SPILLS	NUMBER	NUMBER OF SPILLS
	1001	1050	1960	1970	1971	1972	1973	1974	1975	1976	Volume	Percentage	Number	Percentage
CAUSE OF LEAK OR BREAK - External Impact (1.e., anchor dragging dredging, fishing boards)	160,639	6,000	1909	25,000	80	1	1	19,933	1	4	211,652	88.9%	9	27.4%
- Corrosion	1	ı	1	•		٠	5,000	ı	•	t	5,000	2.1%		4.5%
- Equipment Malfunction	ţ	•	100	ı	•	3,800	•	•	1	•	3,900	1.7%	8	9.1%
- Severe Weather	1	•		•	•	•	•	2,213	ı	•	2,213	26.0		4.5%
- Unknown	99	ı	8,824	70	5,770	100	ŧ	•	1	414	15,243	6.4%	12	54.5%
TOTAL	160,704 6,000	6,000	8,924	25,070 5,850 3,900 5,000 22,146	5,850	3,900	5,000	22,146	0	414	238,008	100.0%	22	100.0%

(a) Spills of 50 barrels or more on OCS and Coastal Waters.

MAJOR U.S. OFFSHORE OIL SPILLS FROM PIPELINES



REF. F5

Causes of oil spills of 1-50 barrels, 1971-75, Gulf of Mexico OCS

Cause	Number of Spills	Total volume (bbl)	Volume (Average	(bbl) pe Maxi- mum	r spi Min mu
Pipeline & Pump Failure:					
Pipeline leaked	63	303.5	4 .82	35	 1.9
Pipeline ruptured	20	161	8.05	32	2
Discharge or transfer line ruptured or coupling failed	54	237	4.39	27	1
Pipeline pump failed	42	211	5.02	20	1
Pig trap leaked	12	35	2.92	10	1
High-low pressure sensor failed	3	18	6.00	8	4
Fuel line leaked	2	3	1.50	2	1
Pump capacity exceeded	1	2	2.00	2	2
Miscellaenous	<u>39</u>	152	3.90	12	1
TOTAL	236	1,122.5	4.76	35	1
Production Platform Equipment Malfunction or Misuse	536	2,286	4.26	50	. 1
Drilling & Workover Mishaps	20	64.5	3.23	10	1
Miscellaneous Equipment Failures & Employee Errors	84	440	5.24	36	. 1
TOTAL	876	3,913	4.47	50	$\overline{1}$

	1971	1972	1973	1974	1975
Total volume of spills					
(bbls)	104	68	87	117	89
Total number of spills	12	12	17	17	25
Average volume per spill	•				
(bbls)	8.67	5.67	5.12	6.88	3.56
% Change in Average Vol.					
from Preceding Year		-34.6%	-9.7%	+21.3%	-48.3%

Cause	No. of Spills	Total Volume (bbls)
Pipeline leaks Pipeline ruptures	63 20	303.5 161
	83	464.5

	spills as % of total # of spills	=	9.5%
Pipeline		=	11.9%
Quantity	The first the object of minimum but obtain	=	5.6 bbls.
Quantity	spilled from pipelines, average per year	=	93 bbls.

REF. F5

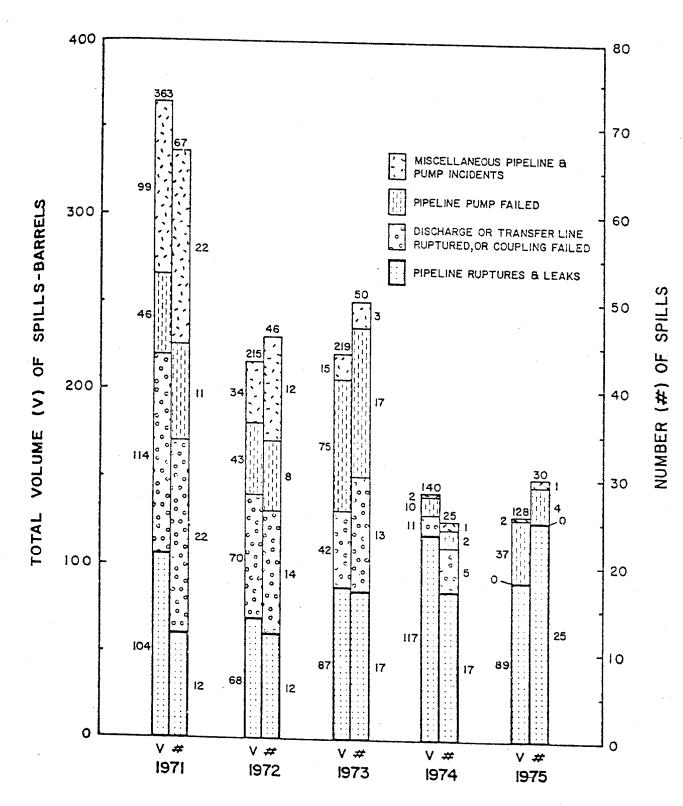
CAUSES OF OIL SPILLS OF MORE THAN 50 BARRELS, 1971-75

GULF OF MEXICO OCS

Cause	Number of Spills	Total Volume (bbl)	Volume (bb] Maximum	l) per spill Minimum
Pipeline leaks and breaks	7*	27,396	19,833	70
Production-platform equipment malfunction or misuse	6	10,925	9,935	75
Drilling and workover mishaps	0	0	0	0
Barge spill (leaks; or oil transfer)	2	7,100	7,000	100
Workboat spillage during unloading of diesel fuel; or collision with platform	3	506	240	100
Other causes	2	320	200	120
Total	20	46,247	_	

*Spills in Federal waters of Gulf of Mexico OCS: 1. Nov. 14, 1971 2. Dec. 17, 1971 3. June 26, 1972 70 bbls. West Delta Blk. 29 Eugene Is. Blk. 238 80 bbls. 100 bbls. West Delta Blk. 79 May 12, 1973 April 17, 1974 5,000 bbls. West Delta Blk. 73 Eugene Is. Blk. 317 19,833 bbls. Eugene Is. Blk. 331 100 bbls. 6. May 21, 1974 2,213 bbls. Main Pass Blk. 73 Sept. 9, 1974 27,396 bbls.

REF. D3, F5



REF. D3,F5

ANNUAL STATISTICS OF SPILLS FROM LIQUID PIPELINE ACCIDENTS (U.S. ONSHORE & OFFSHORE)

														1				
				NUMB	UMBER OF	SPILLS						•	VOLUME OF SPILLS (bbis)	SPILLS (b	bls)			
CAUSE	1968	1969	1970	161	1972	1973	1974	1975	1976	1968	1969	1970	1671	1972	1573	1974	1975	1976
EXTERMAL CORROSIGN	216	155	149	102	7.5	72	25	57	41	69,904	70,878	45,232	29,925	40,475	32,637	21,399	37,073	31,954
INTERNAL CORROSION	9	11	30	22	25	14	15	16	01	7,863	5,725	15,616	12,445	38,988	11,455	3,901	2,853	3,249
OPERATIONAL CAUSES (1)	<u> </u>	15	20	22	24	91	88	22	02	13,237	22,687	32,541	22,830	46,185	63,144	20,957	56,619	40,155
EQUIPMENT MALFUNCTION OR FAILURE (2)		. 8	9	2	20	91	13	27	15	8,146	18,153	16,273	16,266	6,293	11,891	13,474	20,981	5,866
SEVERE WEATHER (3)	4	Ś	_	d)	14	14	6	2	10	6,915	5,535	2,500	4,860	31,799	22,975	6,299	.11,356	4,365
CONSTRUCTION DEFECTS (4) OR MATERIAL FAILURE (5)		28	46	92	62	99	62	52	2	95,758	99,899	45,265	65,646	59,948	169,510	53,485	94,440	51,847
EXTERNAL IMPACT (6)	106	102	75	73	98	74	90	8	78	114,587	96,409	81,531	74,907	123,896	63,600	120,347	116,273	102,587
MISCELLAMEDIUS & UNKNOWN	45	33	20	18	13	Ξ	23	62	19	76,167	24,325	282,891	18,178	13,070	4,153	53,781	9.829	15,014
TOTAL	466	403	347	308	309	273	556	260	209	392,581	343,691	521,849	245,057	360,654	379,365	293,643	319,423	255,037
			SPILLS BY	S BY C	CAUSE AS		PERCENT SPILLS (7)		*****			s so	SPILLS BY CAUSE OF TOTAL VOLUME	AS P	PERCENT SPILLS (7)			
CAUSE	1368	1569	1970 1971	1971	1972		1974	1975	1976	1963	1969	1970			1973	1974	1975	976
EXTERNAL CORROSION	43.3	38.5	42.9	33.1	24.3	26.4	20.3	21.9	19.6	17.8	20.6	8.7	12.2	11.2	8.6	7.3	11.6	12.5
INTERNAL CORROSION	3.2	4.2	8.6	7.1	8.1	5.1	5.9	6.2	8.4	2.0	1.7	3.0	5.1	10.8	3.0	1.3	6.0	1.3
OPERATIONAL CAUSES (1)	2.8	3.7	5.8	7.1	7.8	5.9	10.9	8.5	9.6	3.4	9.9	6.2	9.3	12.8	16.6	7.1	8.3	15.7
EQUIPMENT MALFUNCTION OR FAILURES (2)	3.6	4.5	1.7	3.2	3.2	5.9	3.9	10.4	7.2	2.1	5.3	3.1	9.9	1.7	3.7	4.6	6.6	2.3
SEVERE WEATHER (3)	0.8	1.2	0.3	1.6	4.5	5.1	3.5	8.0	5.9	1.8	1.6	0.5	5.0	8.8	6.1	2.1	3.6	1.7
CONSTRUCTION DEFECTS (4) OR 16.0 MAIERIAL FAILURE	16.0	14.4	13.3	18.2	20.1	20.5	11.3	10.0	9.6	24.4	29.1	8.7	8.92	16.6	44.7	18.2	29.6	20.3
EXTERNAL IMPACT (6)	21.2	25.3	21.6	23.7	27.8	27.1	35.2	31.2	37.3	29.5	28.1	15.6	30.6	34.4	16.8	41.0	36.4	40.2
MISCELLANEOUS & UNKNOWN	9.0	8.2	5.8	5.8	4.2	4.0	9.0	11.2	9.1	19.4	7.1	54.2	7.4	3.6	1.1	18.3	3.1	5.9
TOTAL	1001	1001 100% 100%		100%	1001	1003	1001	100%	1001	2001	100%	1001	1001	1001	1001	1001	100% 1	100%

Incorrect operation by carrier personnel, surge of electricity and surge of flow.

Malfunction of control or relief equipment, malfunction of valve, pump failure, pump packing failure, and tank roof drain leaking.

Heavy rains or floods, cold weather, lightning and landslides.

Defective girth weld, failure of previously welded repairs, and defective weld.

Defective girth weld, failure in river crossing, ruptured or leaking gasket, threads stripped or broken, pipe failed due to buckling, ruptured or leaking seal, pipe coupling failure, defective pipe, stress crack and wrinkle bend split.

Beginnent rupturing line, rupture of previously damaged pipe, freight train derailment, vandalism, and explosives.

REF. F5

ANNUAL AVERAGE VOLUME PER SPILL, BY CAUSE, FROM LIQUID PIPELINE ACCIDENTS

(U.S. ONSHORE & OFFSHORE)

779 325 1,210 2,008 1,435 1,315 790 391 3,632 2,592 1,229 1,220 650 178 5,678 339 777 1974 412 260 748 700 1,844 2,338 1,337 1,147 1,347 AVERAGE VOLUME PER SPILL (bbls) 1,390 453 818 743 378 1973 859 3,947 1,641 3,027 1972 540 1,924 1,560 629 2,271 1,005 1,167 296 1,441 293 999 1,026 972 1,038 962 1,010 1971 1,627 970 1,627 1,087 2,500 1,504 304 984 521 14,145 696 1,512 945 457 337 1,009 1,722 853 1,107 737 1968 324 946 1,730 453 1,693 491 Construction Defects(4) or Material Failure(5) 1,197 1,081 787 Equipment Malfunction or Failures(2) Miscellaneous & Unknown Operational Causes⁽¹⁾ External Corrosion Internal Corrosion External Impact(6) Severe Weather(3) Overall Average

Malfunction of control or relief equipment, malfunction of valve, pump failure, pump packing failure, Incorrect operation by carrier personnel, surge of electricity and surge of flow.

and tank roof drain leaking.

Heavy rains or floods, cold weather, lightning and landslides. 5 4 3

Defective girth weld, failure of préviously welded repairs, and defective weld. Defective pipe seam, failure in river crossing, ruptured or leaking gasket, threads stripped or broken, pipe failed due to buckling, ruptured or leaking seal, pipe coupling failure, defective pipe, stress Equipment rupturing line, rupture of previously damaged pipe, freight train derailment, vandalism, crack and wrinkle bend split. (9)

REF. F5

and explosives

ANNUAL STATISTICS	STATIS	-,	FAILI	JRES OI	GAS	PIPELII	NES (U.	OF FAILURES OF GAS PIPELINES (U.S. ONSHORE AND OFFSHORE), 1970-1976(1)	ORE AN	D OFFSI	10RE),	1970-	$(1)^{\overline{9761}}$	
CAUSE	1970 1971	161	NUMBER 1972	1973	NUMBER OF FAILURES 1972 1973 1974	1975	9761	DISTR 1970	FATLUR IBUTIO	FAILURES BY CAUSE AS PERCENT OF DISTRIBUTION, AND TRANSMISSION & GAT LINE FAILURES(2)	CAUSE TRANSI	AS PER(415510)	CENT OF 8 GAT 1975	CAUSE AS PERCENT OF TRANSMISSION & GATHERING FAILURES(2)
DISTRIBUTION LINES:														
Corrosion 102 Damage by Outside Forces. 462	. 102	120 575	121 630	133 602	108 756	94 744	118 659	15.1 68.3	13.7	13.7	14.9 67.4	10.6 74.3	9.6 76.0	11.4 63.6
Material Failure	53	121	43	95	94	78	115	7.8	13.8	10.2	10.3	9.2	8.0	13.9
Subtotal	929	877	884	893	1017	626	1036	100%	100%	100%	100%	100%	100%	100%
TRANSMISSION & GATHERING LINES:														
Corrosion	181	55 213	74	63 272	78 274	44 237	2115	14.9 52.8	13.4 52.0	18.1 53.5	13.4	17.0 59.6	11.2	21.2 40.3
Construction belief or Material Failure	23	105	36	1111	81	88	180	25.7	25.6	19.6	23.6	17.6	22.3	33.1
Subtotal	343	410	409	471	460	394	543	100%	100%	100%	100%	100%	100%	100%
GAS INDUSTRY TOTAL 1019		1287	1293	1364	1477	1373	1579							

Data for 1968 was not collected and is not reported. 1969 data is incomplete. Percent figures may not total 100% due to rounding off.

PIPELINE CODE COMPARISONS WITH WEST EUROPE COUNTRIES

Gas Pipe Line Code Comparisons

Code	Safety Factor	Design on Min. or Nominal Wall Thickness	Allowable Excess Pressure	Main Line Valve Frequency	Special Remarks	Normal Temperature Range
ANSI B31.8—1968	1.4 to 2.5	Nominal. But may be corrected by de- sign factor F.	Lesser of, 10% overpressure, or pressure to produce 75% of yield.	Every 5 to 20 miles depending on location.	Safety factor varied as function of building density.	
Institute of Petroleum (U.K.)	1.4 or 1.67	Minimum	10% overpressure	Every 10 miles in open country, and at special locations	Both codes specify reduction in safety factor as function of pressures and buildings proximity following	-13°F to 248°F
British Standard Code of Practice CP2010 Part 2 1970.	1.4 or 1.67	Minimum	10% surge	Every 10 miles in open country, and at special locations	principal of USSR National Gas Code (1960) but ANSI B31.8 and IGE procedures accepted as optional.	-13°F to 250°F
Institution of Gas Engineers (U.K.)	1.40 in open country 2.2 close to inhabited building.	Minimum	None	Not greater than 10 miles in open country. Spacing reduced in built-up areas.	Use of 0.72 stress factor limited to population density of one per acre. 0.55 is more common 0.40 in urban areas. Pressures also limited by building proximity.	
Belgium	1.48 to 1.34	Nominal	10% overpressure	At branches and other appropriate locations	:	
International Gas Union Safety Code	1.40 to 2.5 but restriction on yield to ultimate ratio.	Nominal	None	30 km maximum except in desert regions.	Adopted by EEC committee on gas (1965), Based on ANSI B31.3 and USSR Codes which differ primarily on area classification method.	

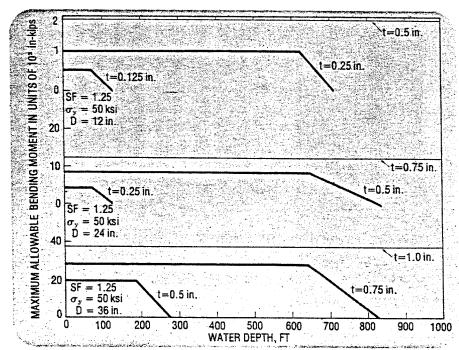
Liquid Pipe Line Code Comparisons

Code	Safety Factor	Designed on Minimum or Nominal Wall	Allowable Excess Pressure	Main Line Valve Frequency	Special Remarks	Normal Temperature Range
ANSI B.31.4 1966	1.4	Nominal	10% surge	At river crossings and as dictated by the terrain.		20°F to 250°F
Institute of Petroleum (U.K.)	1.4	Minimum	10% overpressure	To provide a maximum drainable length of 10 miles and at crossings.		13°F to 248°F
RFF & DIN 2413 (GERMANY)	1.7 average	Minimum	None		Dependent on material, fatigue and temperature conditions SF may increase to 2.5.	
AUSTRIAN ASSOCIATION OF THE MINERAL OIL INDUSTRY	1.4	Minimum	10% overpressure	According to terrain to limit the amount of potential spillage.		-13°F to 248°F
Belgium	1.48 to 1.34	Nominal	10% overpressure	At all branches and as required.		-13°F to 248°F
French	1.22 to 2.28	Minimum	10% surge		Yield valves to which SF applies determined on different principles to ANSI.	up to 248°F
British Standard Code CP2010 Part 2 1970	1.4	Minimum	10% surge	To provide a maximum drainable length of 10 miles and at crossings.		-13°F to 250°F
E.E.C. Draft	Normal areas 1.35 to 1.6 Desert area 1.22	Minimum	10% surge	To limit drainable lengths as dictated by terrain but kept to minimum.	SF may be varied by the "Competent national authority".	-25°C (13°F) +120°C (248°F

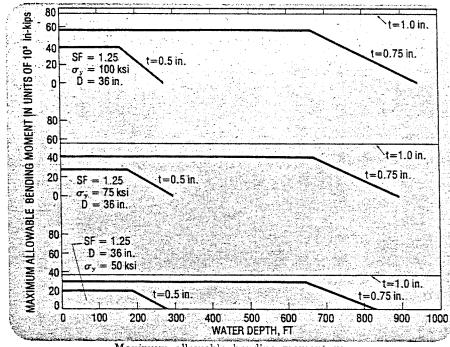
Offshore pipeline burial requirements

Country/Agency	Analiachia code	Pogiuisomente
Country/ Agency	Applicable code	Requirements
UNITED STATES Department of Transportation (DOT)—Office Pipeline Safety Operations (OPSO) Department of Interior (DOI)	49 CFR 192 49 CFR 195	Pipeline to be buried below natural bottom.
—U.S. Geological Survey (USGS)	OCS Order 9	No specific requirement.
—Bureau of Land Management (BLM)	43 CFR 2883	Pipeline must be buried to 3 ft. below the natural seabed out to a water depth of 200 ft.
2. UNITED KINGDOM • Department of Energy (DOE)	Petroleum Pipeline Safety Code 1974 Submarine Pipeline Act, 1975	General guidelines for pipe protection. "The Secretary of State may by regulation make such provisions as he considers appropriate for the purpose of securing the proper construction and preparation in safety operation of pipelines preventing damage to pipelines and securing the safety, health and welfare of persons engaged on pipeline works"
3. NORWAY • Ministry of Petroleum and Energy	Norwegian Petroleum Directorate (NPD), Royal Decrees, 1976	"To the extent reasonable, pipelines shall be protected by burial or by other means to avoid mechanical damage caused by other activities along the route, including fishing and hunting, shipping, and exploration of submarine natural resources. Moreover, the pipelines shall be installed so as not to damage fishing gear."
• Industry Reccommended Practice	Det norske Veritas (DnV), 1976	"The pipeline is to be supported, anchored or buried in such a way that under the assumed conditions it will not move from its as-installed position, apart from movement corresponding to permissible deformation, thermal expansion, and limited amount of settlement after installation."
4. NETHERLANDS • Inspector General of Mines .	Submarine Pipelines for Transport of Gas, 1976	Requirements for burial in shipping lanes or fishing areas to insure safety.
5. JAPAN • Ocean Development Safety Division	Standard for Safety Con- cerning oil and natural gas de- velopment, Part 2, Volume 3	quirements and possible backfill can be imposed for pipelines crossing areas of
6. AUSTRALIA • Standards Association of Australia	Draft-Australia Standard Rules for Submarine Pipelines, 1974	

ALLOWABLE BENDING MOMENT

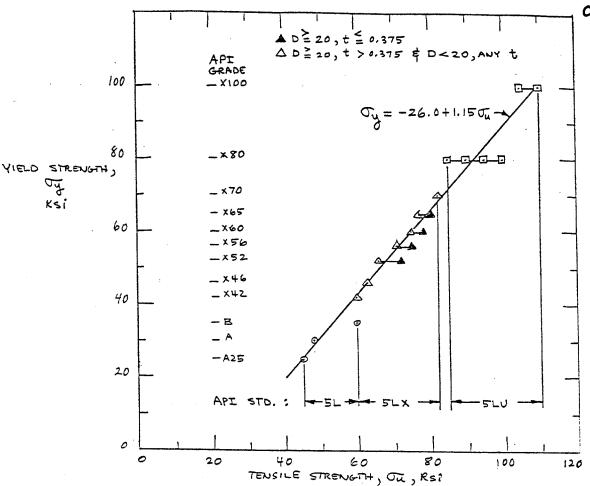


Maximum allowable bending moment vs water depth for various pipeline diameters.

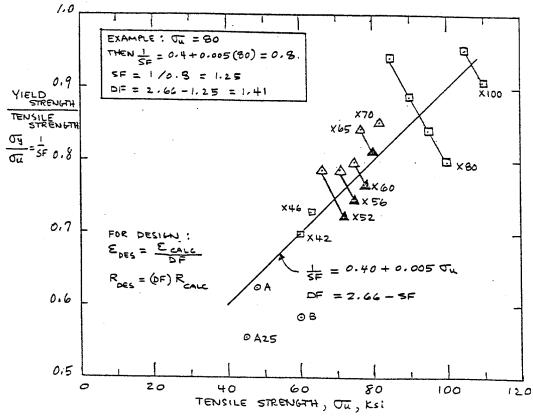


Maximum allowable bending moment vs water depth for various yield stress values.

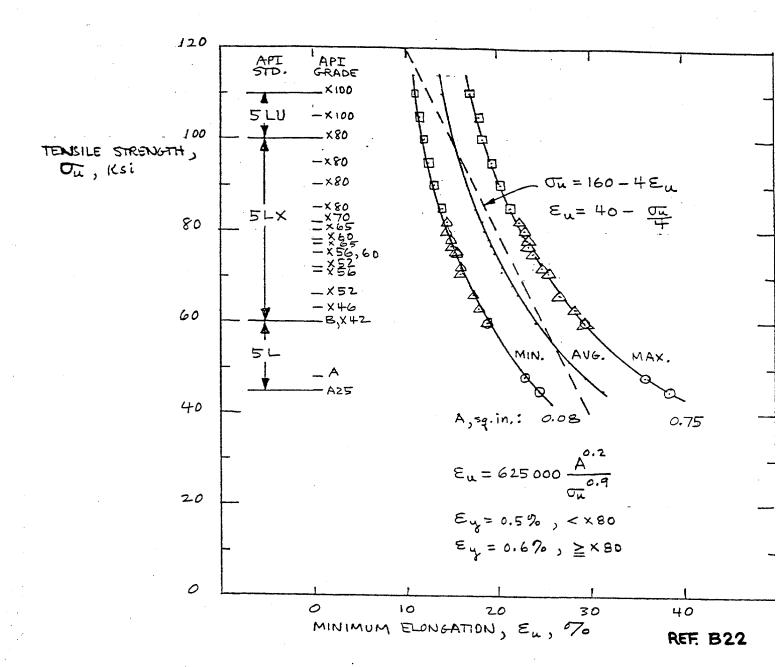




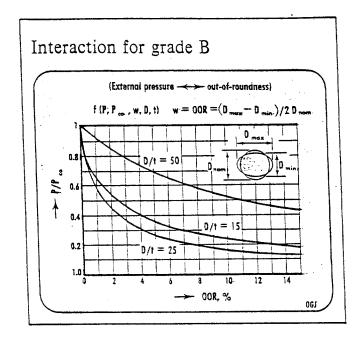
TBUSILE STRENGTH OF APT GRADE PIPE

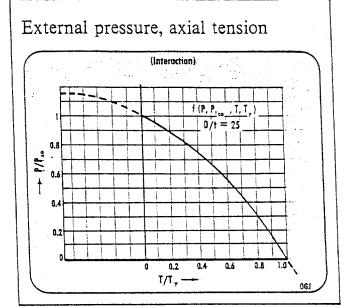


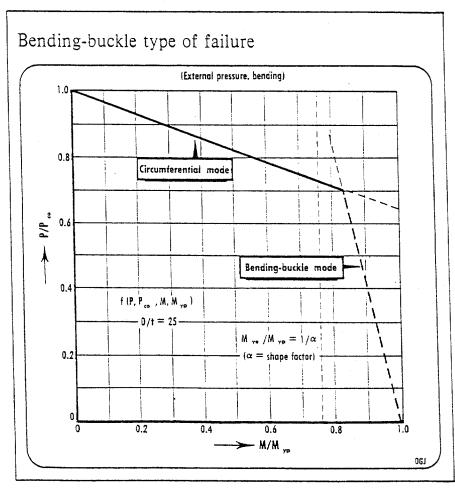
REF. B22



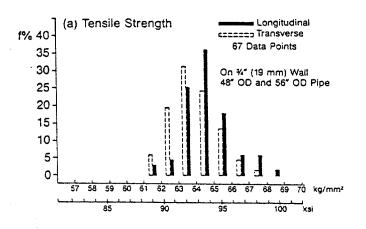
VARIATION OF MINIMUM ELONGATION WITH TENSILE STRENGTH

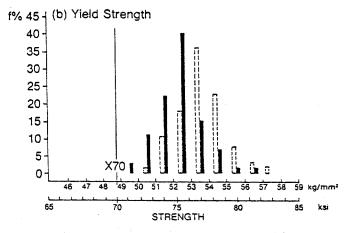


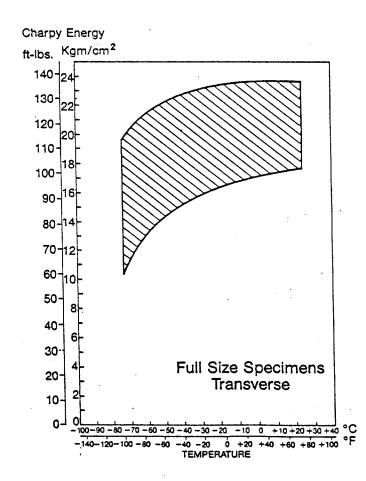


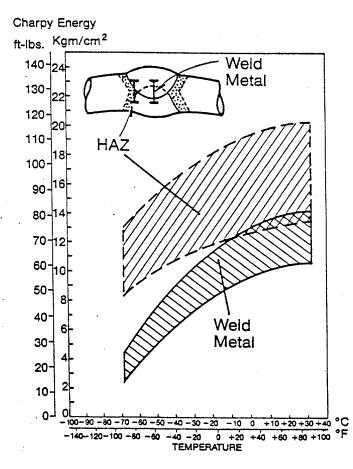


PROPERTIES OF FERRITIC X70 PIPE









REF. C6

PROPERTIES OF SAW X70 PIPE

Specification:

API 5LXX70

Dimensions:

Plate-19.5 mm (0.77 in.) x 436 cm (171.5 in.)

Pipe—1.42 cm (56 in.) OD x 19.5 mm (0.77 in.) WT -60° C (-76° F)

Design Temperature:

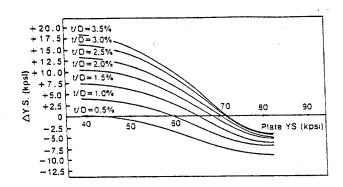
Typical chemical composition

	C	Si	Mn	P	s	Nb	CE*	Remarks
Ladle analysis (%)	0.10	0.25	1.53	0.014	0.006	0.049	0.38	Other microalloy
Check analysis (%)	0.10	0.26	1.54	0.013	0.005	0.051	0.38	added.

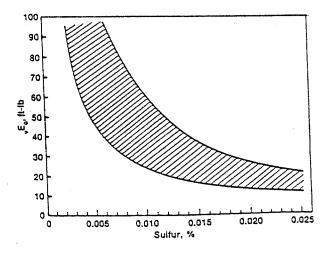
 $^{^{\}circ}$ CE = C + Mn/5 + (Cr + Mo + V)/5 + (Cu + Ni)/15

Tensile test results:

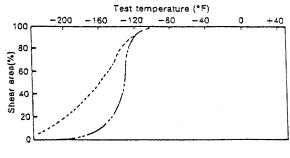
	YS ksi (kg/mm²)	TS ksi (kg/mm²)	YR (%)
Plate	78.2 (55.0)	90.2 (63.4) 93.9 (66.0) 82.0 (57.6) min.	83 83 90 max.

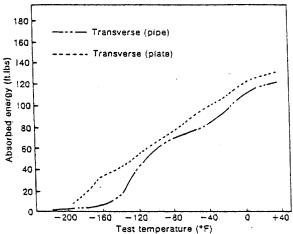


Difference in yield stress between pipe and plate plotted against yield stress of plate as function of t/D.

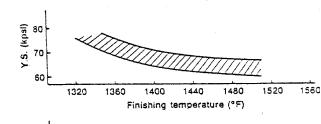


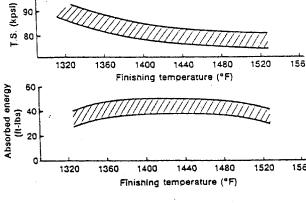
Effect of desulfurization on transverse Charpy

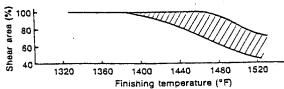




Charpy V-notch transition curves.







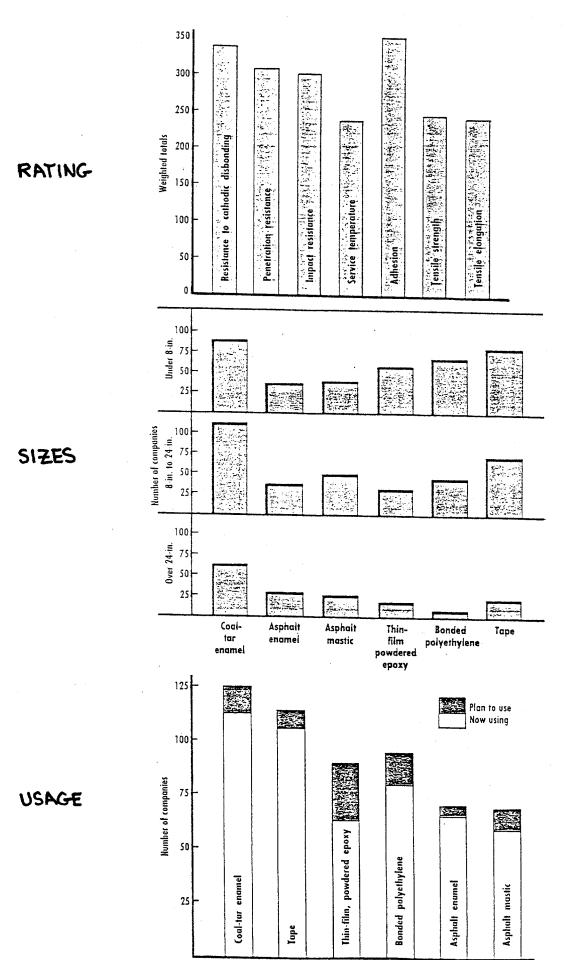
Relation between finishing temperature and med ical properties.

NOMINAL		WALL	INSIDE	FIFTH			AREAS and	WEIGHTS			RADIUS		SEC-
PIPE SIZE and OUTSIDE DIAMETER	API SPECIFI- CATION NUMBER	THICK- NESS	DIAM- ETER	POWER of ID	SURFACE OUT- SIDE	IN- SIDE	Cross-S METAL AREA	ectional FLOW AREA	WEIGI PIPE	WATER	of GYRA- TION	MOMENT of INERTIA	TION MOD- ULUS
inches		inches t	inches d	in. ⁵	sq ft per ft Ao	sq ft per ft A _i	sq in.	sq in. $A_{ m f}$	ib per fi w	ib per fi Ww	inches r _g	in.4 I	in. ³
2 D = 2,375	5L	.083	2.209	52.60	.622	.578	.598	3.83	2.03	1.66	.81	.393	.33
3 D = 3.500	5L 5L 5L	.156 .250 .281	3.188 3.000 2.938	328.5 243 218.9	.916 .916 .916	.835 .785 .769	1.639 2.553 2.842	7.98 7.07 6.78	5.57 8.68 9.66	3.46 3.06 2.94	1.18 1.15 1.14	2.30 3.39 3.71	1.31 1.94 2.12
3½ D = 4,000	5L 5L 5L	.125 .156 .250	3.750 3.688 3.50	741.6 682.3 525.2	1.047 1.047 1.047	.982 .966 .916	1.521 1.884 2.945	11.05 10.68 9.62	5.17 6.41 10.01	4.78 4.63 4.17	1.37 1.36 1.33	2.86 3.49 5.20	1.43 1.74 2.60
D = 4.500	5L 5L 5L 5L	.125 .156 .172 .219	4.250 4.188 4.156 4.062	1387 1288 1240 1106	1.178 1.178 1.178 1.178	1.113 1.096 1.088 1.063	1.931 2.129 2.339 2.950	13.97 13.78 13.57 12.96	6.57 7.24 7.95 10.01	6.05 5.97 5.87 5.61	1.54 1.54 1.53 1.52	4.59 5.03 5.49 6.77	2.04 2.24 2.44 3.01
5 D = 5.563	5L 5L 5L 5L 5L 5L 5L	.083 .156 .188 .219 .281 .312	5.397 5.251 5.187 5.125 5.001 4.939 4.875	4579 3992 3755 3536 3128 2939 2753	1.456 1.456 1.456 1.456 1.456 1.456	1.413 1.375 1.358 1.342 1.309 1.293 1.276	1.420 2.641 3.166 3.666 4.654 4.714 5.631	22.88 21.66 20.13 20.63 19.64 19.16 18.67	4.83 8.98 10.76 12.46 15.82 16.03 19.15	9.91 9.38 9.15 8.93 8.51 8.30 8.08	1.94 1.91 1.90 1.89 1.87 1.86 1.85	5.33 9.66 11.45 13.11 16.28 17.77 19.26	1.92 3.47 4.12 4.72 5.85 6.39 6.92
& D = 6.625	5L 5L 5L 5L 5L 5L 5L 5L	.083 .125 .141 .172 .203 .312 .344 .625	6.459 6.375 6.343 6.281 6.219 6.001 5.937 5.375	11.20T 10.50T 11.30T 9.78T 9.30T 7.78T 7.38T 4.49T	1.734 1.734 1.734 1.734 1.734 1.734	1.691 1.669 1.661 1.644 1.628 1.571 1.554 1.407	4.096 6.188	32.77 31.92 31.60 30.99 30.38 28.28 27.68 22.69	5.80 8.68 9.77 11.86 13.93 21.04 23.08 40.06	14.19 13.82 13.68 13.42 13.15 12.25 11.99 9.83	2.31 2.30 2.29 2.28 2.27 2.24 2.22 2.13	9.13 13.49 15.11 18.17 21.14 30.91 33.58 53.60	2.76 4.07 4.56 5.49 6.38 9.33 10.13 16.18
8 D = 8.625	5L 5L 5L	.312 .438 .562	8.001 7.749 7.501	32.8T 27.9T 23.7T	2.258 2.258 2.258	2.095 2.029 1.964	8.149 11.266 14.236	50.28 47.16 44.19	27.71 38.30 48.40	21.77 20.42 19.14	2.94 2.90 2.86	70.50 94.68 116.3	16.35 21.96 26.96
10 D = 10.750	5L 5L 5L 5L 5L	.344 .438 .562 .625	10.062 9.874 9.626 9.50 9.126	103.0T 93.9T 82.6T 77.4T 63.3T	2.81 2.81 2.81 2.81 2.81	2.63 2.59 2.52 2.48 2.39	11.246 14.190 17.988 19.881 25.352	79.52 76.57 72.78 70.88 65.41	38.24 48.25 61.16 67.60 86.20	33.16 31.51 30.69	3.61 3.59	152.43 189.0 234.2 255.8 315.1	28.36 35.16 43.56 47.59 58.63
12 D = 12,750	5L 5L 5L	.312	12.374 12.126 11.250	290T 262T 180T	3.34 3.34 3.34	3.24 3.17 2.95	7.420 12.192 28.275	120.36 115.49 99.40	25.22 41.45 96.14	50.00		146.4 236.0 511.1	22.97 37.01 80.17
D = 14.000	5L 5L 5L 5L 5L	.344 .562 .688	13.438 13.312 12.876 12.624 12.376	438T 418T 354T 321T 290T	3.67 3.67 3.67 3.67 3.67	3.52 3.49 3.37 3.30 3.24	12.111 14.758 23.726 28.773 33.643	141.8 139.9 130.2 125.2 120.3	41.18 50.18 80.67 97.83 114.39	60.27 56.38 54.20	4.76	285.1 344.3 537 639 734	40.73 49.19 76.66 91.32 104.90
16 D = 16.000	5LX 5L 5L 5L	.562 .625	15.594 14.876 14.750 14.376	922T 729T 698T 614T	4.19 4.19 4.19 4.19	4.08 3.89 3.86 3.76	10.070 27.260 30.190 38.745	191.0 173.8 170.9 162.3	34.30 92.67 102.60 131.70	75.26 73.99	5.46 5.44	314 813 894 1121	39.30 101.70 111.70 140.10
18 D = 18.000	5LX 5L 5L 5LX 5LX	.281 .344 .406	17.562 17.438 17.312 17.188 17.062	1671T 1612T 1555T 1500T 1446T	4.71 4.71 4.71 4.71 4.71	4.60 4.57 4.53 4.50 4.47	12.230 15.642 19.081 22.410 25.830		41.60 53.18 64.88	104.9 103.4 101.9 100.5	6.29 6.27 6.24 6.22 6.20	484 614 744 869 993	53.70 68.24 82.67 96.60 110.40
20 D = 20.000	5L 5L 5LX 5LX 5L 5L	.344 .406 .469	19.438 19.312 19.188 19.062 18.624 18.500	2775T 2686T 2601T 2517T 2241T 2167T	5.24 5.24 5.24 5.24 5.24 5.24	5.09 5.06 5.02 4.99 4.88 4.84	17.408 21.243 25.000 28.780 41.742 45.357	292.9 289.2 285.4 272.4	72.23 85.00 97.80 141.92	128.5 126.8 125.2 123.6 117.9 116.4	6.97 6.95 6.93 6.91 6.83 6.81	846 1026 1200 1373 1949 2105	84.65 102.60 120.00 137.30 194.90 210.50

NOMINAL		WALL	INSIDE	F15-11			REAS and	WEIGHTS	a service cons				
PIPE SIZE	API	THICK-	DIAM-	FIFTH POWER	SURFACE	AREA	Cross-S	ectional	WEIG	HT of	RADIUS	MOMENT of	SEC- TION
OUTSIDE	SPECIFI- CATION	NESS	ETER	of ID	OUT- SIDE	IN- SIDE	METAL AREA	FLOW AREA	PIPE	WATER	GYRA- TION	INERTIA	MOD- ULUS
DIAMETER inches	NUMBER				sq ft	sq ft		100	lb	lb			
A Company of the Comp	and the second	inches t	inches d	in. ⁵ d ⁵	per ft Ao	per ff.	sq in.	sq in. Ai	per ft W	per ft Ww	inches <i>T</i> g	in. ⁴	$\frac{in.^3}{Z}$
	5LX 5L	.219	21.562 21.438		5.76 5.76	5.65 5.61	14.99 19.17	365.1	50.9	:158.1	7.70	889	80.8
	5L	.344	21.312	4397T	5.76	5.58	23.40	360.9 ° 356.7	65.1 79.6	156.3 154.5	7.68 7.66	1131 1373	102.8 124.8
22	5LX 5L	.406 .438	21.124	4206T	5.76 5.76	5.55 5.53	27.54 29.67	352.6 350.5	93.6 100.9	152.7 151.7	7.64 7.63	1606 1725	146.0 156.9
D = 22.000	5LX 5L	.469	21.062 20.876		5.76 5.76	5.51 5.47	31.72 ² 37.85	348.4 342.3	107.9 128.7	150.9 148.2	7.61 7.58	1840 2177	167.2 197.9
	5L 5L	.688 .812	20.624 20.376	3777T	5.76 5.76	5.40 5.33	46.06 54.05	334.1 326.1	156.6 183.8	144.7	7.54 7.50	2619 3038	238.1 276.2
	5L	.281	23.438		6.28	6.14	20.94	431.5	71.2	186.8	8.39	1473	122.8
24	5L 5LX	.344			6.28	6.10 6.07	25.57 30.09	426.8 422.3	86.9 102.3	184.8 182.9	8.37 8.34	1789 2095	149.1 174.6
D = 24.000	5LX 5L	.469 .812	23.062	6524T	6.28 6.28	6.04 5.86	34.67 59.15	417.7 393.2	117.9 201.1	180.9 170.3	8.32 8.20	2401 3982	200.1 331.8
	5L	.250		10.80M	6.81	6.68	20.22	510.7	68.8	221.1	9.10	1677	128.9
26	5L 5L	.281	25.438 25.312	10.70M 10.40M	6.81 6.81	6.66 6.63	22.70 27.73	508.2 503.2	77.2 94.3	220.1 217.9	9.09 9.07	1878 2282	144.5
D = 26.000	5LX 5LX		25.188	10.13M 9.89M	6.81 6.81	6.59 6.56	32.65 37.62	498.3 493.3	111.0	215.8	9.05	2674	205.7
	5L		24.624	9.05M	6.81	6.45	54.71	475.3 476.22	127.9 186.0	213.6 206.2	9.03 8.95	3067 4386	235.9 337
28	5LX 5LX	.250		15.70M 15.60M	7.33 7.33	7.20 7.18	21.80 24.47	594.0 591.3	74.1 83.2	257.2 256.0	9.81 9.80	2099 2351	150 168
D = 28,000	5LX 5LX	.344	27.312 27.188	15.20M 14.86M	7.33	7.15	29.89	585.9	101.6	253.7	9.78	2859	204
D - 20.000	5LX		27.062	14.51M	7.33 7.33	7.12 7.09	35.20 40.56	580.6 575.2	119.7 137.9	251.4 249.1	9.76 9.74	3351 3845	239 275
30	5LX 5LX	.281	29.438 29.312	22.11M 21.64M	7.85 7.85	7.71 7.67	26.24 32.05	680.6 674.8	89.2	294.7	10.51	2897	193
D = 30.000	5LX 5LX	.406	29.188	21.19M	7.85	7.64	37.75	669.1	109.0 128.3	292.2 289.7	10.49	3525 4134	235 276
	5LX	 	29.062 31.500	20.73M 31.01M	7.85 8.38	7.61 8.25	43.51 24.94	663.3	147.9	287.2	10.44	4746	316
32	5LX	.281	31.438	30.71M	8.38	8.23	28.00	779.3 776.2	84.8 95.2	337.4 336.1	11.23 11.21	3143 3523	196 220
D = 32.000	5LX 5LX	.406	31.312 31.188	30.10M 29.51M	8.38 8.38	8.19 8.17	34.21 40.30	770.0 764.0	116.3	333.4 330.8	11.19	4287 5030	268 314
	5LX	+	31.062	28.92M	8.38	8.13	46.46	757.8	158.0	328.1	11.15	5776	361
34	5LX 5LX	.281	33.500 33.438	42.91M 41.80M	8.90 8.90	8.77 8.75	26.51 29.77	881.4 878.2	90.1	381.6 380.3	11.93	3775 4232	222
D = 34.000	5LX 5LX		33.312 33.188	41.02M 40.26M	8.90 8.90	8.72 8.69	36.37 42.85	871.5 865.1	123.7 145.7	377.4 374.6	11.90	5152 6047	303 356
	5LX		33.062		8.90	8.66	49.41	858.5	168.0	371.7	11.86		409
36	5LX 5LX		35.500 35.438	56.38M 55.89M	9.42 9.42	9.29 9.28	28.08 31.53	989.8 986.3	95.5 107.2	428.6 427.1	12.64 12.63	4487 5030	249 280
D = 36.000	5LX 5LX		35.312 35.188	54.91M 53.95M	9.42 9.42	9.25 9.21	38.53 45.40	979.3 972.5	131.0 154.4	424.0 421.1	12.61 12.59	6126	340 400
	5LX		35.062	52.99M	9.42	9.18	52.35	965.5	178.0	418.1	12.56	8265	459
	5LX 5LX	.312		72.94M 72.32M	9.95 9.95	9.79 9.77	36.94 40.70	1097 1093	125.6 138.4	475.0. 475.3	13.33 13.31	6561 7216	345 380
00	5LX 5LX	.375	37.250 37.188	72.32M 71.72M 71.12M	9.95 9.95	9.75 9.74	44.33 47.95	1089 1086	150.7	471.5 470.2	13.30	7846	413
38	5LX	.438	37.124	70.51M	9.95	9.72	51.69	1082	163.0 175.7	468.5	13.28		446 480
D = 38.000	5LX 5LX	.500	37.062 37.000	69.93M 69.34M	9.95 9.95	9.70	55.30 58.91	1078 1075	188.0	466.8 465.5	13.27	9741 10359	513 545
	5LX 5LX		36.876 36.750	68.19M 67.03M	9.95 9.95	9.65 9.62	66.10 73.39	1068 1060	224.7 249.5	462.4 459.0	13.24 13.22	11586 12821	610
	5LX 5LX	.344	39.312	93.89M	10.47	10.29	42.86	1213	145.7	525.2	14.02	8427	421
40	5LX	.406	39.250 39.188	92.42M	10.47 10.47	10.28 10.26	46.68 50.50	1209 1206	158.7 171.7	523.5 522.2	14.01	9900	458 495
40	5LX 5LX	460	39.124 39.062	91.67M 90.94M	10.47	10.24	54.44 58.25	1202 1198	185.1 198.0	520.5 518.7	13.99	10655 11382	533 569
D = 40.000	5LX 5LX		39.000	90.22M	10.47	10.21	62.05 69.63	1194	211.0 236.7	517.0 514.0	13.97	12106 13544	605 677
	5LX	.625			10.47	10.15	77.31	1179	262.8	514.0		14991	750
42	5LX 5LX		41.188		11.00	10.78 10.73	53.05 61.19	1332 1324	180.4 208.1	576.8 573.3		11477	547 629
D = 42.000 48	5LX			<u></u>		 	<u> </u>	╁	+	+	-	+	<u> </u>
D = 48.000	5LX	.406			12.56 12.56	12.35 12.32		1749 1740	206.4	757.3 753.2		3 17194 1 19784	716 824

RELATIONSHIP BETWEEN PIPE DIAMETER, LENGTH, AND VOLUME CONTAINED INSIDE

•	3	•				
INSIDE DIAMETER (in.)			REQUIRED TO 1000 BBL. Kilometers		RELS PER E OF LINE	BARRELS PER KM. OF LINE
2.067		45.63	73.44		22	14
4.026		12.03	19.36		83	52
6.026	•	5.37	8.64		186	116
8.071		2.99	4.82	•	334	208
10.020		1.94	3.13		515	320
12.090		1.33	2.15		750	466
24.000	. *	0.34	0.54		2,954	1,836
28.000		0.25	0.40		4,021	2,499
34.750		0.16	0.26		6,194	3,849
40.000		0.12	0.20		8,207	5,099
46.500	:	0.09	0.15		11,090	6,891
•	ř.	L(mi)	$=\frac{194.965}{D^2}$	V(/mi) = 5.129 D	2
		L(km)	$=\frac{313.766}{02}$	V(/km) = 3.187 D	2
		ָ ("D"	is in inches	.)		



REF. OI

Significant factors for pipeline coatings

		Tyne	of coating —	
Factor	Epoxy powder	Poly- ethylene	Asphait based	Coai-tar based
Thickness* Adhesion (initial) Resistance to disbonding* Upper service temperature* Lower service temperature*† Lower service temperature*§ Impact resistance** Impact resistance** Elongation† Elongation† Tensile strength Water permeability	1+0+0000000+0	00 00 + 0 + + + + 0	+00010001000	+ 000 000 000 000 000 000 000 000 000 0
Oxygen permeability Resistance to biological attack Abrasion resistance Applicability Compatibility with concretes Pipelaying*† Pipelaying*§ Field joint coating* Field joint coatings Cathodic protection considerations* Performance records*\$	001011000000	00000+000+00	000000000+00+	00+000000+00+

^{*}Selected factors of great importance. †Pipeline without concrete weight coating, onshore. §Pipeline with concrete weight coating, offshore.

Examples of published and estimated data for some physical parameters for pipeline coatings

		Соз	ting type		
Property	Asphalt	Coal tar	Epoxy powder	Polyethylene	
Normal thickness, mm	3-7 for enamels; 13-20 for mastics	3-7	0.3-0.5	2-4	
Adhesion of newly applied coatings, approx. figures, MPa	2 estimated	>2 estimated	10-25	> 2 (peel values only)	
Disbonding	variable records	variable records	variable records	susceptible	
Upper service temperature limit (max. operation), °C. Lower service temperature	60-80(90?)	60-80(90?)	90-100(120?)	60-70	
limit, °C. Ultimate elongation, i.e., at	-25?	-30?	-40?	-40?	
break, %	2-5 estimated	2-5 estimated	2-6	500-600	
Water vapor permeability, 10 ⁻⁸ gh ⁻¹ cm ⁻¹ Torr ⁻¹	1.2	1.4 (for a poly- urethane tar)	0.3-1	0.06-0.3	
Water penetration, % of thickness not penetrated	80-100	45-100	25-80	•••	
Oxygen permeability, 10 ⁻¹² cm ² s ⁻¹ Torr ⁻¹		6 (for a poly-	0.5-0.8	10-27	
Impact resistance, Nm Tensile strength, MPa	2-8 2 estimated	urethane tar)	4-88 50	35-50 15	

Current Requirements for Cathodic Protection*					
Area	Water Resistivity (ohm-cm)	Temperature	Turbulence	Typical Current Requirement ma/ft²	
Gulf of Mexico	20	22	Moderate	5	
U.S. West Coast	24	15	Moderate	7	
Cook Injet	50	2	Low	35	
North Sea	26	12	High	10	
Persian Gulf	15	30	Moderate	8	
Indonesia	19	24	Moderate	5	

NACE Standard --- RP-01-76, Pg 11

Amp-Hour Capacity	y Of Anodes*
Anode	Amp Hr/Ib
Aluminum — zinc — mercury	1250-1290
Aluminum — zinc — indium	760-1090
Aluminum — zinc — tin	420-1180
Zinc (MIL-A-18001 H)	379
Magnesium (H1)	500

"NACE Standard --- RP-01-76, Pg 11

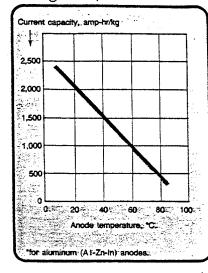
Composition of U.S. Mil. Spec. 18001 H

Metal	Composition, %
Aluminum	0.10 to 0.50
Cadmium	0.025 to 0.150
Iron	max. 0.005
Copper	max. 0.005
Lead	max. 0.006
Silicon	max. 0.125
Zinc	Remainder

Composition of modified zinc anode

Metal	Composition, %
Aluminum	0.1 to 0.2
Cadmium	0.03 to 0.06
Iron	max. 0.002
Copper	max. 0.005
Lead	max. 0.006
Zinc	Remainder

Design capacities*



Potentials for cathodic protection of steel

Metal/Environment	Potentiai (v vs. Ag/AgC seawater ref ence electro
Steel in aerobic environme • positive limit • negative limit	mt -0.80 -1.05
Steel in anaerobic environment • positive limit • negative limit	-0.90 -1.05

Minimum design current densities (ma/m²) fo cathodic protection of bare steel¹

	initial value	Mean value	Final value
North Sea (northern) North Sea (southern)	160 130	120 100	100 90
Arabian Gulf	120	90	90 80
India	120	90	80
Australia	120	90	80 80
Brazil	120	90	80
Gulf of Mexico	100	80	70
Western Africa	120	90	80
Indonesia	100	80	70
Pipelines (burial specified)	50	40	70 30
Risers in shafts with flowing seawater	180	140	120
Risers in shafts with stagnant seawater	120	90	80
Saline mud (ambient temperature)	25	20	15

Anode data for buried pipeline

Anode characteristics	Spacing (p	ipes/anode) 4
Weight, kg	160	320
Outer diameter, m	0.70	0.62
Length, m	0.35	1.4

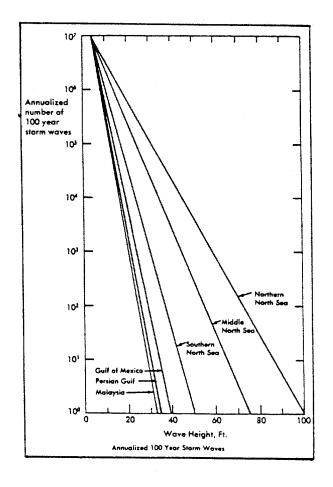
Anode data for unburied pipeline

Anode characteristics	Spacing 3	(pipes/anode) 6
Weight, kg Outer diameter, m Length, m	90 0.6 0.3	

Current capacities found for aluminum anodes in hot saline mud

Publication	Anode (trade name)	Anode temperature, °C.	Test duration, months	Current capacity, amp-hr/kg
Houghton & Ashworth	Gaivalum III*	Ambient (0-20)	6	2.730
	Gaivalum III*	65-77	6/12	617/432
	Ba 778†	65-77	6/12	428/538
	Alanode§	65-77	6/12	348/-
Schrieber & Murray	Galvaium III*	Ambient	0.7-1.3 °	1,984
	Galvaium III*	38	0.7-1.3	1,984
	Galvaium III*	60	0.7-1.3	1,323
	Galvaium III*	82	0.7-1.3	880
Jensen, Rygh & Setre	Alanode§	80	1	466

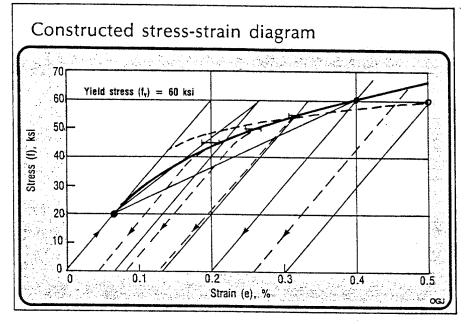
^{*}Galvalum is a trademark of The Dow Chemical Co. †Ba 778 is a British Aluminium patented alloy. §Alanode is a Mitsubishi Metal Corp. patented alloy.

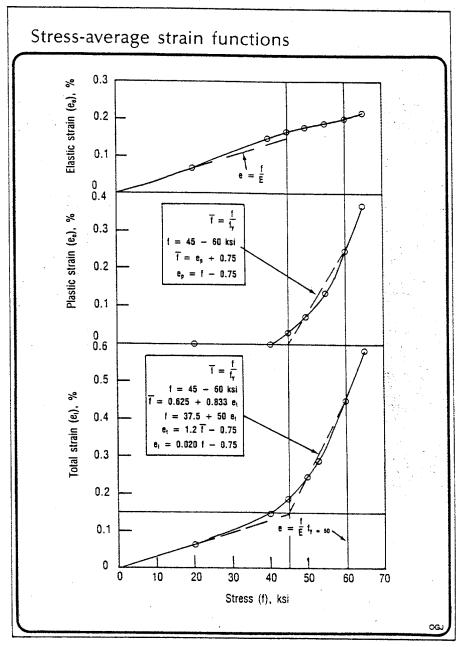


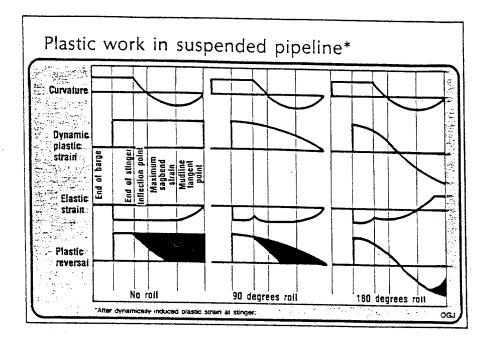
Design Cr Storm Case Area	riteria fo I Malaysia	2	3	torm 4 Southern North Sea	5 Middle North Sea	6 Northern North Sea
Maximum wave	33	35	39	50	75	100
Maximum one minute wind gust, knot	62	53	74	100	100	100
Design Severity Compared To:						
Malaysia		0.92	1.15	1.56	1.83	2.08
Persian Gulf Gulf of Mexico Southern North Sea Middle North Sea Northern North Sea	0.87 0.64	0.80 0.59 0.50 0.44	1.25 1 0.73 0.63 0.55	1.70 1.36 1 0.86 0.75	2.00 1.60 1.17 1 0.88	2.27 1.82 1.33 1.14

Annualized	100	Year	Storm	Wave	Height	Distribution
				•		

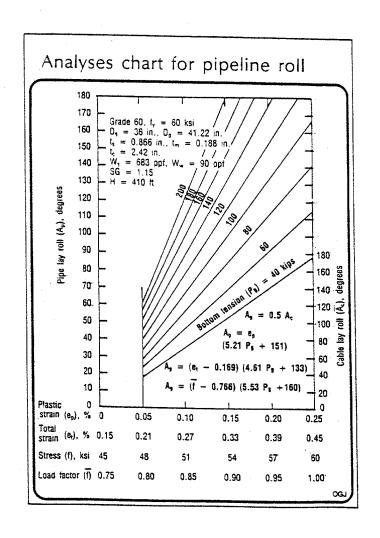
		Wave	Height,	ff.		
Number of Waves	Malaysia				Middle North Sea	Northern North Sea
107	. 4	4	4	4	4	4
106	. 8	9	9	10	14	- 18
105	. 12	13	14	17	24	31
104	. 16	. 1 <i>7</i>	19 .	. 22	34	45
103	. 21	22	24	30	44	59
102	. 25	26	29	37	55	73
101	. 29	30	34	44	65	86
100	. 33	35	39	50	75	100
Note: Assumes one 3	0 minute ma	ximum storm	at a single	location in	100 years.	







an and a merculy parameter of the



LOGARITHMIC 359-112 KEUFFELA PSSER CO. WATERIALA. 2 x 3 CYCLES

e - Arrista i ser i e p

USING O = K & PER REF BI3

n = E = STRAIN HARDENING COEFFICIENT

ENGINEERING OR NOMINAL VALUES: $\sigma = \frac{P}{Ai}$, $\varepsilon = \frac{L_f - L_i}{L_i} = \frac{L_f}{L_i} - 1$

WITH YOLUME CONSTANT IN PLASTICITY, Y= V; OR ALL; = A+L+

THEREFORE TRUE STRESS IS: $\vec{\sigma} = \frac{P}{A_s} = \frac{\sigma}{A_s} = \frac{\sigma}{A_$

TRUE STRAIN IS: $\overline{\epsilon} = \int_{L_i}^{L_f} \frac{dL}{L} = \ln \left(\epsilon + 1 \right)$

TO DETERMINE VALUE FOR " :

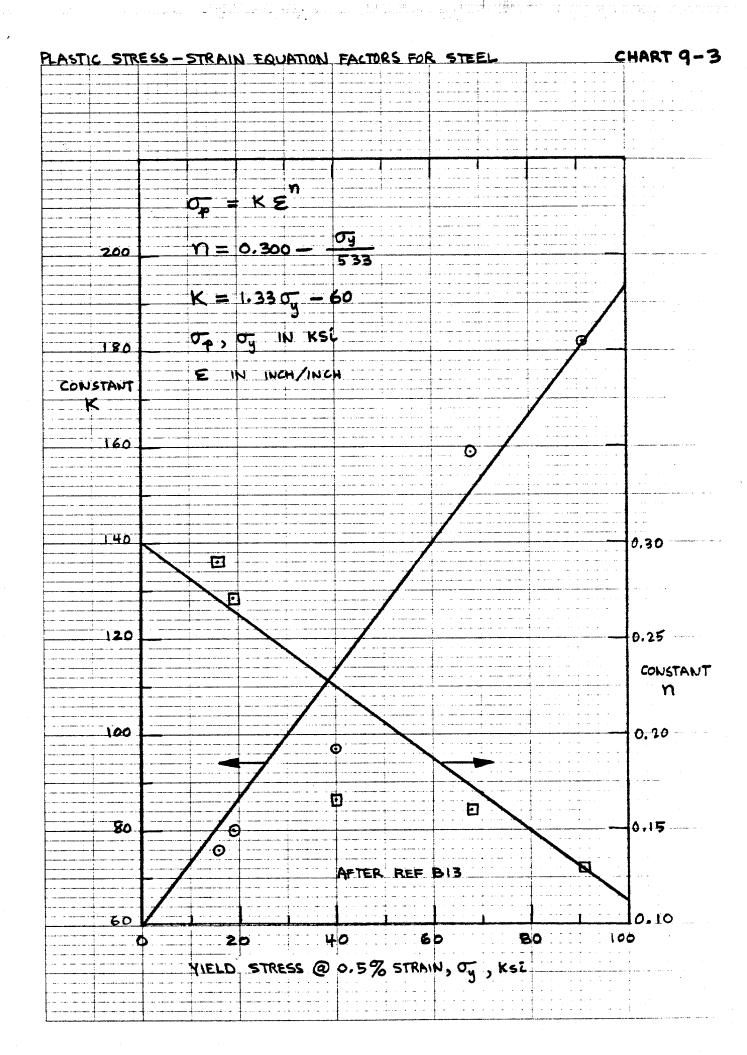
PLASTIC INSTABILITY AT 2P = 0

 $P = \overline{\sigma} A_i$, $\overline{z} = \ln \frac{A_i}{A_f} \Rightarrow A_i = A_o e^{\overline{z}}$ $P = \sigma A_i e^{-\overline{z}}$

dp=Aie do-JAie le=0

AF = F @ PMAX

O=KE" = do = KnE" => n= Eu



	REF. VI NOMINAL VALUES	TRUE
ULTIMATE STRESS, KSC	91.3	132
YIELD STRESS, KSI	70.2	70.5
ULTIMATE STRAIN, in./in.	0.443	0.366
YIELD STRAIN, in./in.	0.005	0.005
o de la companya de La companya de la co		

5 = KE"

log
$$\overline{\sigma} = \log K + n \log \overline{\epsilon}$$

2.1205 = $\log K + n (-0.4365)$
1.1848 = $\log K + n (-2.3010)$

n = 0.2723 = 0.146 ys 0.17 from General Graph

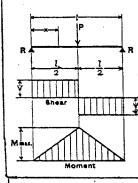
1.864

VS 0.366 TRUE ULTIMATE STRAIN

$$K = \frac{\sigma}{\epsilon} = \frac{132}{0.366} = 152$$

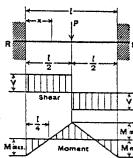
BEAM DIAGRAMS AND FORMULAS For various static loading conditions

A. SIMPLE BEAM—CONCENTRATED LOAD AT CENTER



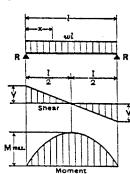
	Equivalent Tabular Load = 2P
	R = V
	M max. (at point of load) $=\frac{Pl}{4}$
7	M_X (when $x < \frac{l}{2}$) $= \frac{P_X}{2}$
	Δ max. (at point of load) = $\frac{PI^3}{48EI}$
	Δ_X (when $x < \frac{l}{2}$) $\approx \frac{P_X}{48El} (3l^2 - 4x^2)$

B. BEAM FIXED AT BOTH ENDS—CONCENTRATED LOAD AT



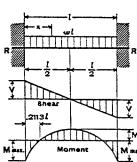
Equivalent Tabular Load			- P
R = V			- <u>P</u>
M max. (at center and end	3)		= <u>P1</u>
$M_X = \left(when x < \frac{l}{2} \right)$.			$=\frac{p}{8}(4x-l)$
Amax. (at center)			P/3 192E1
Δ_{X} (when $X < \frac{l}{2}$).			

C. SIMPLE BEAM-UNIFORMLY DISTRIBUTED LOAD



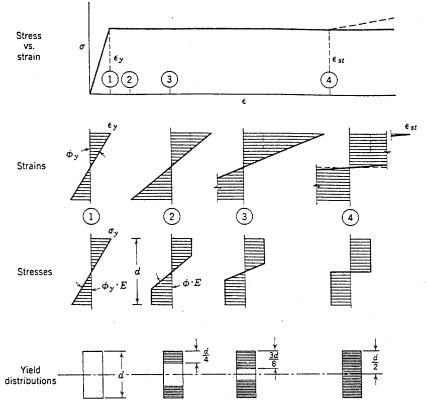
-deliant labelat cost	•	•	•	- w:
R = V	• , •			$=\frac{wl}{2}$
Vx	• •			$= w\left(\frac{l}{2} - x\right)$
M max. (at center)		•		= wi ² 8
M _X				$=\frac{wx}{2}(l-x)$
Δmax. (at center)				$=\frac{5 wl^4}{384 El}$
Δχ				$= \frac{wx}{24F1} (l^3 - 2lx^2 + x^3)$

D. BEAM FIXED AT BOTH ENDS—UNIFORMLY DISTRIBUTED LOADS

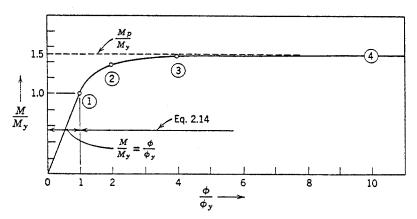


•
$R = V$ $= \frac{wl}{3}$
- .
$\forall x \dots = w\left(\frac{l}{2} - x\right)$
$M \max \left(\text{ at ends} \right) \dots \dots = \frac{wl^2}{12}$
•
M_1 (at center) = $\frac{wl^2}{24}$
24
M_X = $\frac{w}{12}$ (6 $lx - l^2 - 6x^2$)
12 (0.4 - 1 - 0.4 -)
Δ max. (at center) = $\frac{wl^4}{384El}$
384EI
wx² /,
$\Delta_{x} \qquad \ldots \qquad = \frac{wx^{2}}{24Ei} (l-x)^{2}$

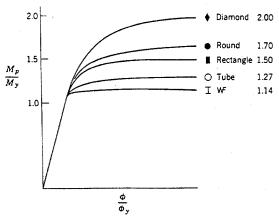
Equivalent Tabular Load . . . $=\frac{2wi}{3}$



Plastic bending of rectangular beam.



Nondimensional moment-curvature relationship for rectangular beam.

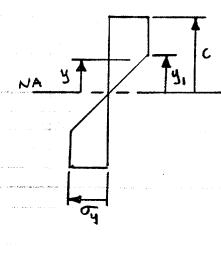


Variation in the shape factor for various cross-sectional forms.

WHEN
$$y < y_1$$
, $\frac{\sigma}{y} = \frac{\sigma y}{y_1} \Rightarrow \sigma = \frac{y}{y_1} \sigma y$

WHEN y > y, ,
$$\sigma = \sigma_y = c$$

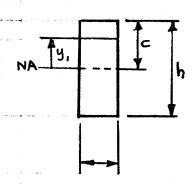
$$M = \int \sigma y dA = 2 \int_{y_{1}}^{y_{1}} \frac{y}{\sigma_{1}} \sigma_{1} y dA + 2 \int_{y_{1}}^{y_{2}} \sigma_{2} y dA + 2 \int_{y_{1}}^{y_{2}} \sigma_{3} y dA + 2 \sigma_{3} \int_{y_{1}}^{y_{2}} dA + 2 \sigma_{3} \int_{y_{1}}^{y_{2}} dA$$



FOR A RECTANGULAR SECTION,

$$M = \frac{2\sigma_{4}}{y_{1}} \left(\frac{by_{1}^{3}}{3} \right) + 2\sigma_{4} b (c - y_{1}) \left(\frac{c + y_{1}}{2} \right)$$

$$= \sigma_{4} \left(bc^{2} - \frac{b}{3} y_{1}^{2} \right)$$



FOR A FULLY PLASTIC MOMENT, 4, = 0 AND

$$M_p = bc^2 \sigma_y = \frac{bh^2}{4} \sigma_y$$

THEREFORE
$$\frac{M_p}{Me} = 1.5$$

TO LOCATE ZERO MOMENT :

$$M_{\times} = \frac{W}{12} (6L \times -L^2 - 6 \times^2) = 0 \implies 6 \times^2 - 6L \times +L^2 = 0$$

$$x = \frac{-b \pm \sqrt{b^2 + 4ac}}{2a} = \frac{6L \pm \sqrt{36L^2 + 46L^2}}{2(6)} = \frac{6L \pm L\sqrt{12}}{12} = 0.5L \pm 0.288L = 0.212L, 0.788L$$

TO LOCATE 3 MMAX :

$$x = \frac{6L \pm \sqrt{36L^2 - 4(6)(5)L^2}}{2(6)} = 0.5L \pm 0.440L = 0.060L, 0.940L$$

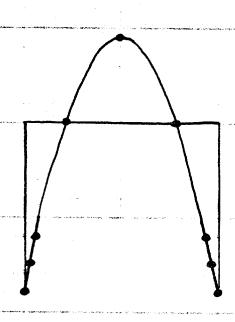
TO LOCATE 5 MMAX .

$$6Lx^2 - L^2 - 6x^2 = -\frac{5}{6}L^2 \implies x = 6L \pm \sqrt{36L^2 - 24\frac{L^2}{6}} = 0.5 \pm 0.471 = 0.029L, 0.971L$$

MOMENT VS LOCATION RATIOS:

$$\frac{\Delta \frac{1}{6} M_{MAX}}{\Delta \frac{1}{3} M_{MAX}} = 2 \approx \frac{x_{1/3}}{x_{1/6}} = \frac{0.060}{0.029}$$

THEREFORE APPROXIMATELY LINEAR MOMENT FROM M= 2 MMAX TO FIXED END.



STRAIN RATIOS,
$$\frac{\mathcal{E}_{c}}{C} = \frac{\mathcal{E}_{y}}{y_{i}}$$

FROM GEOMETRY,
$$\varphi = \frac{1}{R} = \frac{d\theta}{dx} = \frac{\varepsilon_c}{C} = \frac{\varepsilon_y}{y_I} = \frac{\sigma_y}{\varepsilon y_I}$$

$$M = \frac{dy}{y_1} \left(bc^2 - \frac{b}{3} y_1^2 \right) y_1$$

$$\frac{Q\Phi}{dx} = \frac{dy}{Ey_1} = \frac{M}{Ey_1(bc^2 - \frac{b}{3}y_1^2)} = \frac{M}{Eby_1(c^2 - \frac{y_1^2}{3})} = \frac{1}{R}$$

COMBINING ABOVE RELATIONS (SEE P.29, REF BIH OR P.147, REF N5)

$$M = \sqrt{\frac{bc^2 - \frac{b}{3}(\sqrt[q]{R})^2}{E}} \quad \text{or} \quad \frac{M}{M_y} = \frac{3}{2} \left[1 - \frac{1}{3}\left(\frac{R}{R_y}\right)^2\right]}$$

ALTERNATELY
$$R = \frac{ET}{M_y} \sqrt{3 - \frac{2M}{M_y}}$$

IN TERMS OF STRESS:

OR IN TERMS OF STRAIN :

$$\sigma_{x} = \frac{\mu E}{(1+\mu)(1-2\mu)} e + \frac{E}{1+\mu} \epsilon_{x}$$

O4 = ---

IN THE CASE OF PLANE STRESS, OF = 7/2 = 7/2 = 0, AND

$$o_{x} = \frac{E}{1-\mu^{2}} (E_{x} + \mu E_{y})$$

$$\sigma_{y} = \frac{E}{1-\mu^{2}} (\epsilon_{y} + \mu \epsilon_{x})$$

IN THE CASE OF PLANE STRAIN, E2 = 142 = 12x =0 , AND

g sale sales sale

$$\sigma_{\tilde{z}} = \frac{ME}{(1+M\chi_{1-2M})} (E_{\chi} + E_{\gamma})$$

WHERE $e = E_X + E_Y + E_Z$ AND $G = \frac{E}{2(1+\mu)}$

FOR THREE DIMENSIONAL STRESS :

OR IN TERMS OF STRESS COMPONENTS ONLY:

OR IN TERMS OF STRAIN COMPONENTS ONLY

IN THE CASE OF PLANE STRESS, Q=Ty2=T2x=0 AND

IF UNIT DEPTH AND
$$\nabla_{p} = K E^{n}$$

$$\xi = 4K \iint_{X y} e^{n+1} dx dy = 4K \left(\frac{E_{m}}{E}\right)^{n+1} \int_{X=0}^{\infty} \left(1 - \frac{x^{2}}{X_{0}^{2}}\right)^{n+1} dx dy$$

$$= 4K \left(\frac{2E_{m}}{t}\right)^{n+1} \int_{X=0}^{\infty} \left(1 - \frac{x^{2}}{X_{0}^{2}}\right)^{n+1} \frac{y^{n+2}}{y^{2}} dx$$

$$= 4K \left(\frac{2E_{m}}{t}\right)^{n+1} \int_{X=0}^{\infty} \left(1 - \frac{x^{2}}{X_{0}^{2}}\right)^{n+1} \frac{y^{n+2}}{y^{2}} dx$$

$$y = \frac{t}{2} \sqrt{\frac{x}{X_{0}^{2}}}$$

$$= \frac{4K}{n+2} \left(\frac{2E_{m}}{t}\right)^{n+1} \int_{x=0}^{\infty} \left(1 - \frac{x^{2}}{x_{o}^{2}}\right)^{n+1} \left(c^{n+2} - \left[\frac{1}{2}\left(\frac{x}{x_{o}}\right)^{n+2}\right]\right) dx$$

$$= \frac{4K}{n+2} \left(\frac{2E_{m}}{t}\right)^{n+1} \int_{x=0}^{\infty} \left(1 - \frac{x^{2}}{x_{o}^{2}}\right)^{n+1} - \left(\frac{t^{2}}{4}\frac{x}{x_{o}}\right)^{\frac{n+2}{2}} \left(1 - \frac{x^{2}}{x_{o}^{2}}\right)^{\frac{n+1}{2}} dx$$

TO INTEGRATE, USE BINOMIAL EXPANSION :

$$(1\pm v)^{m} = 1\pm mx + \frac{m(m-1)}{2!}v^{2} \pm \frac{m(m-1)(m-2)}{3!}v^{3} + \cdots$$

SUBSTITUTE V = X2 , m = n+1 INTO EXPANSION , MULTIPLY TERMS ,

COMBINE UNITS, THEN INTEGRATE OVER LIMITS.

FOR AN ELASTIC TRIAXIAL STRESS STATE :

$$(\sigma_1 - \sigma_2)^2 + (\sigma_2 - \sigma_3)^2 + (\sigma_3 - \sigma_1)^2 = 2 \sigma_{yu}^2$$

OR IN TERMS OF STRAIN

$$(\epsilon_1 - \epsilon_2)^2 + (\epsilon_2 - \epsilon_3)^2 + (\epsilon_3 - \epsilon_1)^2 = 2(1+\mu)^2 \epsilon_{yu}^2$$

FOR ELASTIC ANALYSES , POISSONS RATIO, M, IS 0.3 AND

$$(\epsilon_1 - \epsilon_2)^2 + (\epsilon_2 - \epsilon_3)^2 + (\epsilon_3 - \epsilon_1)^2 = 3.38 \epsilon_{yu}^2$$

FOR PLASTIC ANALYSES, POISSONS RATIO, M, IS 0,5 AND

$$(\xi_1 - \xi_2)^2 + (\xi_2 - \xi_3)^2 + (\xi_3 - \xi_1)^2 = 4.50 \xi_{yu}^2$$

HUBER-VON MISES - HENCKY MAXIMUM ENERGY OF DISTORTION FAILURE THEORY :

$$(\sigma_1 - \sigma_2)^2 + (\sigma_2 - \sigma_3)^2 + (\sigma_3 - \sigma_1)^2 = 2\sigma_y^2$$

THE RADIAL STRESS IS NEGLIGIBLE, I.e.

FOR A SECTION OF PIPE WITH UNRESTRAINED ENDS : E = - LE

THEN FOR A PIPE WITH RESTRAINED ENDS: 02 = 4 07

$$50 \left(\sigma_1 - \mu \sigma_1\right)^2 + \left(-\mu \sigma_1\right)^2 + \sigma_1^2 = 2 \sigma_y^2$$

USING POISSONS RATIO OF U = 0.3 : 0.79 07 = 07 OR 07 = 1.26 04

SO THE ALLOWABLE PRESSURE BY VON MISES IS ABOUT 26% GREATER THAN

CALCULATIONS BY PLANE STRESS ANALYSES,

PER TIM OSHENKO FORMULAS (REF. T4) FOR BUCKLING OF THIN TUBES:

FOR EXTERNAL PRESSURE ONLY ,
$$p = \frac{2E}{1-\mu^2} \left(\frac{t}{D}\right)^3$$

IF
$$\mu = 0.3$$
 THEN $p = 2.20 E \left(\frac{t}{D}\right)^3$; $\sigma = 1.21 E \left(\frac{t}{D}\right)$

DUE TO RESTRAINT OF A PIPELINE TO FREELY EXPAND LONGITUDIONALLY,

$$1 = \frac{p}{p_{c}} + \frac{0.15p(\frac{1}{5})}{1.21E(\frac{1}{5})} = \frac{p}{p_{c}} \left[1 + \frac{0.15 + (2.20)E(\frac{1}{5})^{3}}{1.21E(\frac{1}{5})} \right] = \frac{p}{p_{c}} \left[1 + 0.272 + \frac{1}{1.21E(\frac{1}{5})} \right]$$

THEREFORE LONGITUDIONAL RESTRAINT CAUSING BIAXIAL LOADS HAS NEGLIGIBLE EFFECT

$$A_i = \pi D^2/4$$

$$A_f = A_i - 4 \frac{1}{2} \frac{D}{2} \frac{D}{2} = A_i - \frac{D^2}{2}$$

$$\Delta A = A_i - A_f = \frac{D^2}{2} = \Delta V/L$$

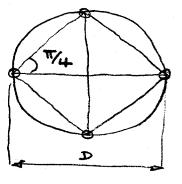
$$W_e = \frac{PD^2}{Z}$$

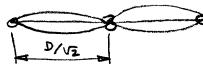
$$M = \left(\sigma \pm \chi \pm \frac{1}{2}\right) = \frac{\sigma + 2}{4}$$

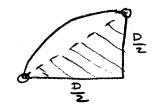
$$E_{d} = \left(\frac{\sigma t^{2}}{4}\right)\left(2\pi\right) = \frac{\sigma t^{2}\pi}{2}$$

$$\frac{\sigma t^2 \pi}{2} = \frac{\beta D^2}{2}$$

$$P_p = \pi \sigma \frac{t^2}{D^2}$$









$$W_e = P\Delta V = P + \frac{D^2}{4}$$

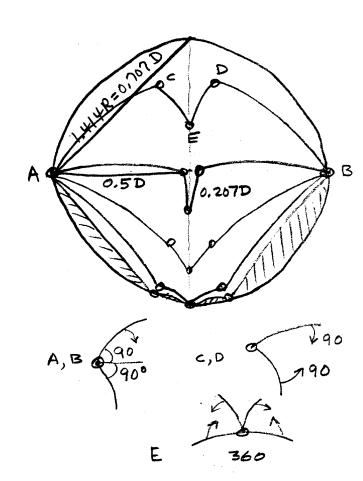
$$M = (-\frac{t}{2})\frac{t}{2} = \frac{-t^2}{4}$$

$$\triangle \Phi = 2(180) + 2(180) + 360 = 3(360)$$

$$= 3 (2\pi) = 6\pi$$

$$P_{\pi}D^2 = \frac{3}{2}\pi\sigma t^2$$

$$P = K + \frac{1}{D^2} \stackrel{?}{=} \sigma + \frac{1}{D^2} = KG\sigma \left(\frac{t}{D}\right)^2$$



1. FLAGGS LINE , NORTH SEA

H = 500 ft.,
$$\sigma_y$$
 = 60 ksi, D = 36.0 in., t = 0.866 in., $\frac{D}{t}$ = 41.5

$$P_{c} = \frac{2E}{1-\mu^{2}} \left(\frac{t}{D}\right)^{3} = \frac{2,19(3^{\frac{7}{2}})}{0.714^{\frac{5}{2}}} = 920 \text{ psi}$$

$$P_p = \pi \sigma_y \left(\frac{t}{D}\right)^2 = 3.14 \left(\frac{6^{\frac{t}{2}}}{1.72^{\frac{3}{2}}} = 109 \text{ psi}$$

$$\frac{p_c}{p_p} = \frac{920}{109} = 8.44$$

2. COGNAC LINE , GULF OF MEXICO

$$P_{\omega} = 444$$
, $P_{c} = 7670$, $P_{p} = 347$, $\frac{P_{c}}{P_{p}} = 22.1$

and the second of the second o

element and the second of the

WORK AT EACH END OF FIXED BEAM IS MOMENT TIMES ANGLE, THEREFORE

$$= 0.392 \text{ Gy t}^2$$

$$\frac{M}{M_p} = \frac{\sigma_y \left[\frac{bt^2}{4} - \frac{byo^2}{3}\right]}{\sigma_y \left[\frac{bt^2}{4}\right]} = 1 - \frac{4}{3} \frac{yo^2}{t^2}, PARABOLIC$$

TO GET VARIATION OF YO(x):

$$x = ay_0^2 = x_0 = a\left(\frac{t}{2}\right)^2 \Rightarrow a = \frac{4x_0}{t^2}$$

TO GET VARIATION OF & (x):

$$\varepsilon_{c} = a + b \times^{2}$$
, $\varepsilon_{m} = a + b (0)$, $a = \varepsilon_{m}$
 $\varepsilon_{y} = a + b \times^{2}$, $b = \varepsilon_{y} - \varepsilon_{m}$

$$\Rightarrow \xi_{e} = \xi_{m} + \xi_{\frac{q}{2} - \xi_{m}} \times^{2}$$

TO GET VARIATION OF E(y):

$$\frac{\varepsilon_{c}}{\varepsilon_{0}} = \frac{c}{y_{0}} = \frac{\varepsilon_{c}}{\varepsilon} = \frac{c}{y} \Rightarrow \varepsilon = \frac{y}{c} \varepsilon_{c}$$

COMBINING ABOVE:
$$\mathcal{E}(x,y) = \left(\mathcal{E}_m + \frac{\mathcal{E}_y - \mathcal{E}_m}{x^2} \times^2\right) \frac{y}{\mathcal{E}}$$

SINCE
$$\frac{\epsilon_y}{\epsilon_m} \approx 0$$
 THEN USE $\epsilon(x,y) = \epsilon_m \left(1 - \frac{x^2}{x_0^2}\right) \frac{y}{\epsilon}$

INTEGRATING OVER ONE HALF OF ONE END OF BEAM OF UNIT DEPTH :

=
$$+ \frac{x^2}{4} = + \frac{x^2}{4}$$

$$= 2 \operatorname{Oy} \underset{C}{\mathcal{E}_{m}} \int_{x=0}^{x_{0}} \left(c^{2} - \frac{t^{2} \times}{4 \times_{0}} - c^{2} \times \frac{x^{2}}{x_{0}^{2}} + \frac{t^{2} \times x^{3}}{4 \times_{0}^{3}} \right) dx$$

$$= \sigma_y \, \varepsilon_m \, t \, \left(\times_o \, - \, \frac{\times_o}{2} \, - \, \frac{\times_o}{3} \, + \, \frac{\times_o}{4} \, \right)$$

$$L = 1.414 \frac{D}{2} = 0.707 D$$

$$E_{m} = 22.1 \pm \frac{1}{D}$$

FOR PIPELINE,
$$E_2 = 0.5 \, \epsilon_1$$
, $\frac{\epsilon_3}{\epsilon_1} \approx 0$

$$\Longrightarrow \varepsilon_{yu} = \sqrt{\frac{1.5}{4.5}} \ \varepsilon_1 = 0.577 \ \varepsilon_1 = 0.577 \ \varepsilon_m$$

THERE FORE EQUIVALENT UNIAXIAL MINIMUM ULTIMATE ELONGATION IS :

$$E_{yu} = 0.577 (22.1) \frac{t}{D} = 12.75 \frac{t}{D}$$

EXAMPLE 1: D=36, t=0.866,
$$\frac{D}{t}$$
=41.5, Eyu = $\frac{12.75}{41.5}$ =0.307 = 30.7% FLAGGS LINE

EXAMPLE 2:
$$D=12.75$$
, $t=0.625$, $P=20.4$, $E_{yu}=\frac{12.75}{20.4}=0.625=62.5%$ COGNAC LINE

$$\frac{P}{E} = \frac{2E}{1-\mu^2} \left(\frac{t}{D}\right)^3 , \quad \frac{D}{t} > 30$$

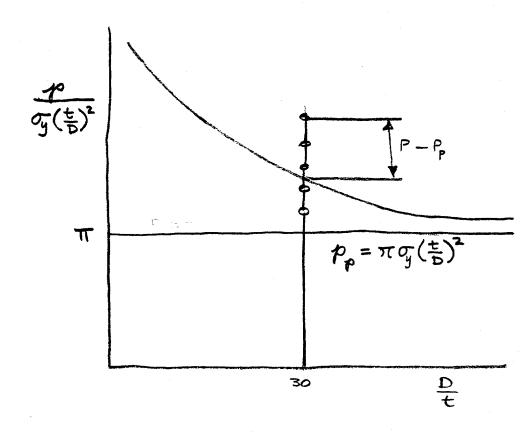
FOR STEEL,
$$\mu = 0.28$$
, $E = 3^{\frac{7}{2}} \Rightarrow \frac{2E}{1-\mu^2} = \frac{2(3^{\frac{7}{2}})}{1-0.28^2} = 2.170(3^{\frac{7}{2}}) = 6.51^{\frac{7}{2}}$

$$\frac{P_{c}}{P_{p}} = \frac{6.51^{\frac{7}{5}} (\frac{t}{0})^{\frac{3}{5}}}{\pi \sigma \frac{t^{\frac{3}{5}}}{D^{\frac{3}{5}}}} = \frac{2.07^{\frac{7}{5}}}{\sigma} \frac{t}{D}$$

$$\frac{P_c}{P_p} = \frac{2.07^{\frac{7}{2}}}{42^{\frac{3}{2}}} \frac{t}{D} = 4.93^{\frac{2}{2}} \frac{t}{D}$$

IF
$$\frac{D}{t} = 30$$
, $\frac{P_c}{P_p} = \frac{4.93^{\frac{2}{30}}}{30} = 0.164^{\frac{2}{30}} = 16.4$

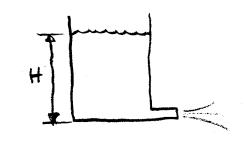
BUT IN PRACTICE,
$$\frac{P_c}{P_b} = \sim 5-7$$

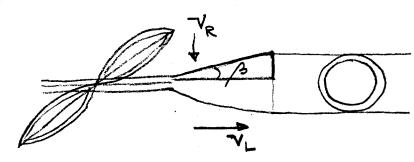


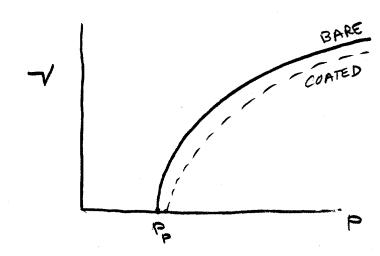
$$V_R = \sqrt{2gH}$$

$$H = \frac{\Delta P}{Y} = \frac{P - P_0}{Y}$$

$$\tan \beta = \frac{\sqrt{R}}{\sqrt{L}} \approx \frac{1}{3} - \frac{1}{6}$$







Pw = XH

Pp < Pc

Pp < Pw BY MECHANKS

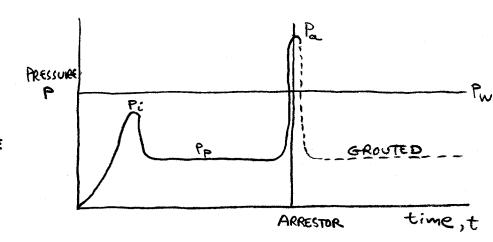
Pp < Pi DUE TO CONCRETE

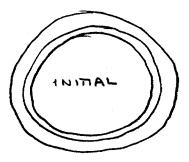
P. < B DUE TO OVALITY

PW < P BY DESIGN

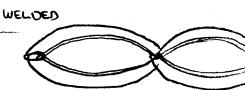
PW < Pa BY DESIGN

Pa>Pe

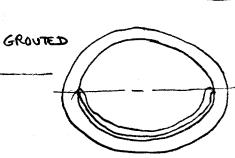




Pa ≈ Pe



Pa < ~ 4 Pp -



$$P_p = \pi \sigma_{yp} \left(\frac{t}{D}\right)^2$$

$$P_a = \pi \nabla_a \left(\frac{h}{D}\right)^2$$